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@Boston Physics Seminar

Disclaimer:

This talk may contain highly speculative opinions, please use at your own discretion. Opinions are my own.

Overview

Al

- Al Capabilities and Limitations
- When are Al capable/incapable?

Humanity

- Camps and survival strategies

Myself

- My own survival strategies (my research)

Al Capabilities and Limitations

March 16, 2023

GPT-4 Technical Report

OpenAI*

Abstract

We report the development of GPT-4, a large-scale, multimodal model which can accept image and text inputs and produce text outputs. While less capable than humans in many real-world scenarios, GPT-4 exhibits human-level performance on various professional and academic benchmarks, including passing a simulated bar exam with a score around the top 10% of test takers. GPT-4 is a Transformer-based model pre-trained to predict the next token in a document. The post-training alignment process results in improved performance on measures of factuality and adherence to desired behavior. A core component of this project was developing infrastructure and optimization methods that behave predictably across a wide range of scales. This allowed us to accurately predict some aspects of GPT-4's performance based on models trained with no more than 1/1,000th the compute of GPT-4.

arXiv: 2303.08774

March 24, 2023

Sparks of Artificial General Intelligence: Early experiments with GPT-4

Sébastien Bubeck Varun Chandrasekaran Ronen Eldan Johannes Gehrke Eric Horvitz Ece Kamar Peter Lee Yin Tat Lee Yuanzhi Li Scott Lundberg Harsha Nori Hamid Palangi Marco Tulio Ribeiro Yi Zhang

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Abstract

Artificial intelligence (AI) researchers have been developing and refining large language models (LLMs) that exhibit remarkable capabilities across a variety of domains and tasks, challenging our understanding of learning and cognition. The latest model developed by OpenAI, GPT-4 [Ope23], was trained using an unprecedented scale of compute and data. In this paper, we report on our investigation of an early version of GPT-4, when it was still in active development by OpenAI. We contend that (this early version of) GPT-4 is part of a new cohort of LLMs (along with ChatGPT and Google's PaLM for example) that exhibit more general intelligence than previous AI models. We discuss the rising capabilities and implications of these models. We demonstrate that, beyond its mastery of language, GPT-4 can solve novel and difficult tasks that span mathematics, coding, vision, medicine, law, psychology and more, without needing any special prompting. Moreover, in all of these tasks, GPT-4's performance is strikingly close to human-level performance, and often vastly surpasses prior models such as ChatGPT. Given the breadth and depth of GPT-4's capabilities, we believe that it could reasonably be viewed as an early (yet still incomplete) version of an artificial general intelligence (AGI) system. In our exploration of GPT-4, we put special emphasis on discovering its limitations, and we discuss the challenges ahead for advancing towards deeper and more comprehensive versions of AGI, including the possible need for pursuing a new paradigm that moves beyond next-word prediction. We conclude with reflections on societal influences of the recent technological leap and future research directions

arXiv: 2303.12712

Write poems

Write LaTeX codes for plotting

GPT-4

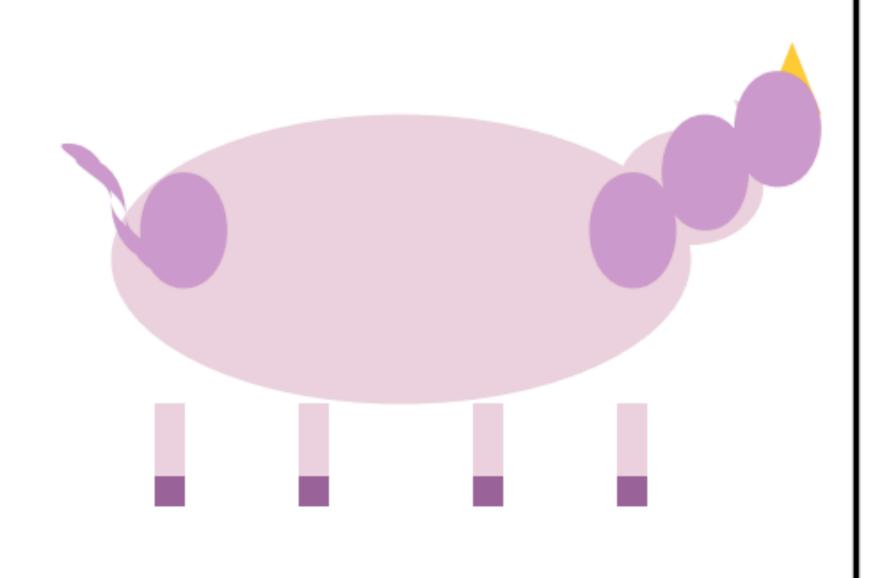
Prompt: Can you write a proof that there are infinitely many primes, with every line that rhymes?

GPT-4:

Yes, I think I can, Though it might take a clever plan. I'll start by noting Euclid's proof, Which shows that primes aren't just aloof. Assume we have a finite list, Of primes, and that none have been missed. Multiply them all together, And add one, just to be clever. The result will be a number, That has no prime factors, oh wonder! But every number has a prime, That divides it, it's just a matter of time. So we've found a contradiction, And our finite list needs eviction. There must be infinitely many primes, And that's the end of my rhyming lines.s

Prompt: Draw a unicorn in TiKZ.

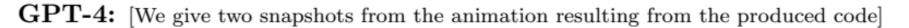
GPT-4: [Produces LATEX compiling to following picture.]

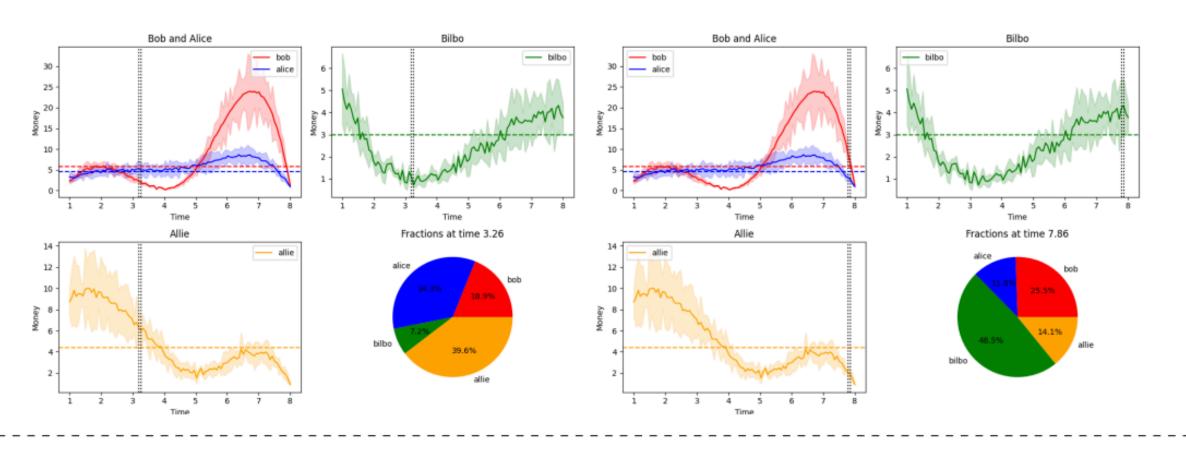


Write python codes for plotting

Prompt: Can you generate a pyplot for the following data: x = [1, 3, 5, 6, 8], y1 = [2, 3, 5, 18, 1], y2 = [3, 5, 6, 8, 1], y3 = [5, 1, 2, 3, 4], y4 = [9, 7, 2, 3, 1]. I want y1, y2 to be in the same plot, but y3 is in another plot next to that plot, y4 is in below. I want the legend of y1 to be "bob", y2 to be "alice", y3 to be "bilbo", y4 to be "alie". I want the x-axis to be labeled with "time" and y axis to be labeled with "money". I want to add a 10 %-40% random error bar to each curve, through all times (including non-integers). I want smoothed curves to show the plot, and smoothed error bar. Do not use linear interpolation, use smooth interpolation! I want to also add some small zig-zag to the smoothed curve to make it look more real. I want to put a baseline as the mean of each line. I want to put a pie chart below indicating the fraction of the four people in each time step. I also want an animation to show how the fractions are changing in the pie chart in **continuous time**. Interpolate the missing fractions! I also want vertical line animation in other three plots to match the pie chart. I want the fanciest plot. Please add as many fancy things as possible.

Here is a possible code to generate a pyplot for the following data, with some comments to explain the steps:





Do simple math problems

```
Prompt: Suppose g(x) = f^{-1}(x), g(0) = 5, g(4) = 7, g(3) = 2, g(7) = 9, g(9) = 6 what is f(f(f(6)))?
```

GPT-4: There are different ways to approach this problem, but one possible method is to use the fact that $g(x) = f^{-1}(x)$ implies that f(g(x)) = x for any x in the domain of g. That is, applying f to both sides of the equation $g(x) = f^{-1}(x)$ gives $f(g(x)) = f(f^{-1}(x)) = x$. This means that we can undo the effect of f by applying g, and vice versa. Using this idea, we can try to find f(6) by looking for the value of x such that g(x) = 6. From the given information, we see that g(9) = 6, so f(6) = f(g(9)) = 9. Similarly, we can find f(9) by looking for the value of x such that g(x) = 9. We see that g(7) = 9, so f(9) = f(g(7)) = 7. Finally, we can find f(7) by looking for the value of x such that g(x) = 7. We see that g(4) = 7, so f(7) = f(g(4)) = 4. Therefore, f(f(f(6))) = f(f(9)) = f(7) = 4.

Solve LeetCode problems

```
GPT-4:
class Solution(object):
    def numberOfPaths(self, grid, k):
         :type grid: List[List[int]]
        # Define MOD as 10**9 + 7
        MOD = 10**9 + 7
        # Get the dimensions of the grid
        m = len(grid)
        # dp[i][j][value] represents the number of paths where the sum of the elements on the path has a remainder of value when divided
        dp = [[[0] * k for _ in range(n)] for _ in range(m)]
        \# Base case: the first cell has only one path and its value is grid[0][0] \% k
        for i in range(m)
            for j in range(n):
                # Skip the first cell
                if i == 0 and j == 0:
                    continue
                # Loop through all possible remainders
                for value in range(k):
                    # The number of paths to the current cell with the current remainder is equal to the sum of:
                    # - The number of paths to the top cell with the previous remainder
                    # - The number of paths to the left cell with the previous remainder
                    # The previous remainder is equal to the current remainder minus the current value, plus k if it is negative
                    prev = (value - grid[i][j]) % k
```

Compose music

```
GPT-4
Can you compose a short tune (say four to eight bars) using ABC notation?
There are many possible ways to compose a short tune in abc notation, but here is one example:
T:Example Tune
M:4/4
L:1/8
|:G2AB c2BA | G2AB c2c2 | edcB c2BA | G4-G2z2 :|
|:c2de f2ed | c2de f2f2 | g2fe d2cB | c4-c2z2 :|
This tune has two four-bar phrases, each repeated once, forming an A part and a B part. The key is C
Can you describe the tune in musical terms?
Here is one possible description:
The tune starts with a rising arpeggio of the tonic chord (C major), followed by a descending scale that
returns to the tonic. This pattern is repeated, but the second time the scale continues to the higher
tonic note. The first phrase ends with a long tonic note.
The second phrase begins with a similar pattern, but using the subdominant chord (F major) instead of
the tonic. The second time, the scale continues to the higher subdominant note. The phrase ends with a
stepwise descent to the tonic, followed by a long tonic note.
The A part and the B part have a similar structure, but use different chords and ranges. The tune has a
simple and catchy melody, with a clear sense of tonality and rhythm.
I like part A, but maybe part B is just a bit too similar to part A, making the song repetitive. How
about beginning part B with a descending arpeggio instead of a rising one?
Sure, that would create some contrast and variation. Here is one possible way to do that:
T:Example Tune
M:4/4
L:1/8
|:G2AB c2BA | G2AB c2c2 | edcB c2BA | G4-G2z2 :|
|:f2ed c2BA | f2ed c2c2 | g2fe d2cB | c4-c2z2 :|
That's much better. Now how about making this into a duet, can you add a second staff for this with a
bass accompanying the melody?
One possible way to write a second staff for this tune is to use root notes and fifths of the chords, as
well as some passing notes, to create a simple accompaniment. Here is an example in abc notation, with
the second hand bass on the lower staff:
X:1
T:Example Tune
M:4/4
L:1/8
|:G2AB c2BA | G2AB c2c2 | edcB c2BA | G4-G2z2 :|
|:f2ed c2BA | f2ed c2c2 | g2fe d2cB | c4-c2z2 :|
|:C,2C,2 G,2G,2 | C,2C,2 G,2G,2 | F,2F,2 E,2E,2 | C,4-C,2z2 :|
|:F,2F,2 C,2C,2 | F,2F,2 C,2C,2 | G,2G,2 F,2F,2 | E,2C,2 G,2C,2 :|
```

Explain jokes

Example of GPT-4 visual input:

User What is funny about this image? Describe it panel by panel.



Source: https://www.reddit.com/r/hmmm/comments/ubab5v/hmmm/

GPT-4 The image shows a package for a "Lightning Cable" adapter with three panels.

Panel 1: A smartphone with a VGA connector (a large, blue, 15-pin connector typically used for computer monitors) plugged into its charging port.

Panel 2: The package for the "Lightning Cable" adapter with a picture of a VGA connector on it.

Panel 3: A close-up of the VGA connector with a small Lightning connector (used for charging iPhones and other Apple devices) at the end.

The humor in this image comes from the absurdity of plugging a large, outdated VGA connector into a small, modern smartphone charging port.

Table 3. Example prompt demonstrating GPT-4's visual input capability. The prompt consists of a question about an image with multiple panels which GPT-4 is able to answer.

4 Mathematical abilities

In this section we begin to assess how well GPT-4 can express mathematical concepts, solve mathematical problems and apply quantitative reasoning when facing problems that require mathematical thinking and model-building. We demonstrate that GPT-4 represents a jump in that arena too with respect to previous LLMs, even when compared to specially fine-tuned for math models such a Minerva. As it seems, however, GPT-4 is still quite far from the level of experts, and does not have the capacity required to conduct mathematical research.

The reader is called into caution that interpreting the results in this section correctly is a difficult exercise. As we will see, GPT-4 can answer difficult (indeed, competitive) high-school level math questions, and can sometimes engage in meaningful conversation around advanced math topics. Yet, it can also make very basic mistakes and occasionally produce incoherent output which may be interpreted as a lack of *true understanding*. Its mathematical knowledge and abilities can depend on the context in a seemingly arbitrary way.

Prompt:

A rain barrel collects water off the roof of a house during three hours of heavy rainfall. The height of the water in the barrel increases at the rate of $r(t) = 4t^3e^{-1.5t}$ feet per hour, where t is the time in hours since the rain began.

At time t = 1 hour, the height of the water is 0.75 foot. What is the height of the water in the barrel at time t = 2 hours?

GPT-4:

GPT-4 uses a correct approach (integration by parts), but produces a wrong final answer due to a calculation error

If we can find a function F such that F'(t) = r(t), then F(2) - F(1) is the amount that the height of the water increases from t = 1 to t = 2.

To find such a function F, we can use the technique of integration by parts, which says that if u and v are differentiable functions, then

$$\int u dv = uv - \int v du$$

Applying this to $r(t) = 4t^3e^{-1.5t}$, we can choose $u = t^3$ and $dv = 4e^{-1.5t}dt$, so that $du = 3t^2dt$ and $v = -\frac{8}{3}e^{-1.5t}$. Then we have

$$\int 4t^3 e^{-1.5t} dt = -\frac{8}{3}t^3 e^{-1.5t} - \int -\frac{8}{3}e^{-1.5t} 3t^2 dt$$

Simplifying and applying integration by parts again, we can choose $u = t^2$ and $dv = -\frac{8}{3}e^{-1.5t}dt$, so that du = 2tdt and $dv = \frac{16}{9}e^{-1.5t}$. Then we have

$$\int 4t^3 e^{-1.5t} dt = -\frac{8}{3}t^3 e^{-1.5t} + \frac{16}{9}t^2 e^{-1.5t} - \int \frac{16}{9}e^{-1.5t} 2t dt$$

...

We begin with a simplification of a question which appeared in the 2022 International Mathematics Olympiad (IMO).

GPT-4

Prompt:

Suppose g is a continuous smooth function such that for every x > 0, there is **one and only one** y > 0 such that $g(x) + g(y) \le 2xy$. Can you prove that $g(x) = x^2$?

GPT-4:

There are a few possible ways to approach this problem, but one possible method is as follows:

- Assume, for the sake of contradiction, that g(x) is not equal to x^2 for some x > 0.
- Then, either $g(x) < x^2$ or $g(x) > x^2$ for that x.
- If $g(x) < x^2$, then let y = x. Then $g(x) + g(y) = 2g(x) < 2x^2 = 2xy$.
- If g(x) + g(y) < 2xy, then g(x) + g(y) is strictly less than the upper bound of 2xy for positive x and y.
- This means that there is some room to increase y slightly and still satisfy the inequality $g(x) + g(y) \leq 2xy$.
- For example, let $y' = y + \epsilon$, where ϵ is a small positive number such that g(x) + g(y') < 2xy. This is possible because g is continuous and smooth, so it does not have any jumps or kinks that would prevent such a choice of epsilon.
- Then, y' is another positive number such that $g(x) + g(y') \le 2xy'$, which contradicts the assumption that y is the one and only one positive number that satisfies this condition given x.
- Therefore, if $g(x) < x^2$, then g(x) + g(y) cannot be strictly less than 2xy, and it must be equal to 2xy.
- If $g(x) > x^2$, then let y^* be the unique positive solution of g(x) + g(y) = 2xy. Then $g(y^*) < (y^*)^2$, since otherwise we would have $g(x) + g(y^*) > 2xy$, which contradicts the existence of y^* given x.
- But then, by the same argument as before, we can let $x = y = y^*$ and obtain a contradiction, since $g(y) + g(y) = 2g(y) < 2y^2 = 2yy$, which contradicts the uniqueness of y given y.
- Therefore, g(x) must be equal to x^2 for all x > 0, as required.

Solving it requires a more creative approach, as there is no clear strategy for beginning the proof. For example, the decision to split the argument into two cases $(g(x) > x^2)$ and $g(x) < x^2$ is not an obvious one, nor is the choice of y * (its reason only becomes clear later on in the argument). Furthermore, the solution demands knowledge of calculus at the undergraduate level. Nevertheless, GPT-4 manages to produce a correct proof.

formula.

GPT-4

Human: Can you remind me what a k-SAT problem is?

AI: A k-SAT problem is a type of logical problem that involves finding a way to assign truth values (true or false) to a set of variables that appear in a collection of clauses, each of which consists of a disjunction (logical OR) of exactly k literals. A literal is either a variable or its negation. For example, (x_1 OR NOT x_2 OR x_3) is a clause with k=3 and three literals.

The problem is to find an assignment of truth values to the variables that satisfies (makes true) all the clauses in the collection, or to determine that no such assignment exists. This is called the satis fiability problem, or SAT for short.

Human: What's the most obvious way (the first thing you would refer to when teaching a class) to solve a k-SAT problem?

AI: There are different ways to approach the k-SAT problem, but one of the most obvious and straightfor ward methods is to use brute force, or exhaustive search. This means trying all possible combinations of truth values for the variables, and checking if any of them satisfies all the clauses. For example, if there are n variables, there are 2^n possible combinations to try.

Human: Ok, great. Now, given the instance of a k-SAT problem suppose that I define a graph where each vertex refers to a variable in the instance, and two vertices are connected by an edge if and only if the two variables appear in the same clause. Suppose that for a certain instance, the graph I just described has two connected components of size n/2 each. In this case, is there a more efficient way to solve the k-SAT instance?

AI: Yes, there is a more efficient way to solve the k-SAT instance in this case. Since the graph has two connected components, this means that the clauses can be partitioned into two subsets, such that each subset only involves the variables in one component. Therefore, the k-SAT instance is equivalent to solving two independent k-SAT instances, each with n/2 variables. This reduces the number of possible combinations to try from 2^n to $2^{n/2} + 2^{n/2}$, which is much smaller for large n. In general, the more dis connected the graph is, the easier the k-SAT instance becomes, because it can be decomposed into smaller subproblems.

Human: Now suppose that the graph has only one connected component, but if you were to remove one single edge, then it would have two connected components. Can you suggest an algorithm in this case? AI: One possible algorithm in this case is to use a divide and conquer strategy. First, identify the edge that, if removed, would split the graph into two components. Then, assign a truth value to one of the variables that are connected by that edge, and solve the resulting k-SAT instance recursively. If the instance is satisfiable, then return the solution. If the instance is unsatisfiable, then assign the opposite truth value to the same variable, and solve the k-SAT instance recursively again. If the instance is still unsatisfiable, then return that the original k-SAT instance is unsatisfiable. This algorithm reduces the number of possible combinations to try from 2^n to $2^{n-1} + 2^{n-1}$, which is still better than brute force. However, this algorithm depends on finding the edge that splits the graph, which may not be easy in general.

Human: Can you generalize this principle to the case that the graph has q edges which, if removed, would split the graph into p connected components?

AI: The general principle is similar, but more complicated. The idea is to assign truth values to the variables that are connected by the q edges that split the graph, and solve the resulting k-SAT instance recursively for each possible assignment. If any of the assignments leads to a satisfiable k-SAT in stance, then return the solution. If none of the assignments leads to a satisfiable k-SAT instance, then return that the original k-SAT instance is unsatisfiable. This algorithm reduces the number of possible combinations to try from 2^n to $2^q \times 2^{(n-q)/p}$, which is better than brute force if q is small and p is large. However, this algorithm also depends on finding the q edges that split the graph, which may be hard in general.

Human: Note that the complexity that you wrote is only correct in the case that all connected components are of the same size. Can you find a more general formula?

AI: Yes, you are right. The more general formula is $2^q \times \sum_i 2^{n_i}$, where n_i is the number of variables in the i-th connected component, and the sum is over all p components. This is because each component has 2^{n_i} possible combinations to try, and the q edges that split the graph have 2^q possible assignments. This formula is equal to the previous one if all n_i are equal to (n-q)/p.

GPT-4 demonstrates understanding of the concepts from graph theory and algorithms. It is able to reason about an abstract graph construction, which relates to a constraint satisfaction problem, and deduce correct conclusions about the SAT problem (to the best of our knowledge, this construction does not appear in the mathematical literature). The conversation reflects profound understanding of the undergraduate-level mathematical concepts discussed, as well as a significant extent of creativity. Although GPT-4 makes a mistake in one instance (writing 2n-1 rather than 2n/2), the subsequent conversation demonstrates that this error does not reflect a lack of understanding. Rather, GPT-4 seems to have made an error in a manner similar to a human typo, as it later provides the correct generalization of the

Where it could go wrong

Error type	Percentage of wrong solutions
Arithmetic mistakes (including counting) Misunderstanding the problem statement Wrong approaches	$egin{array}{cccccccccccccccccccccccccccccccccccc$

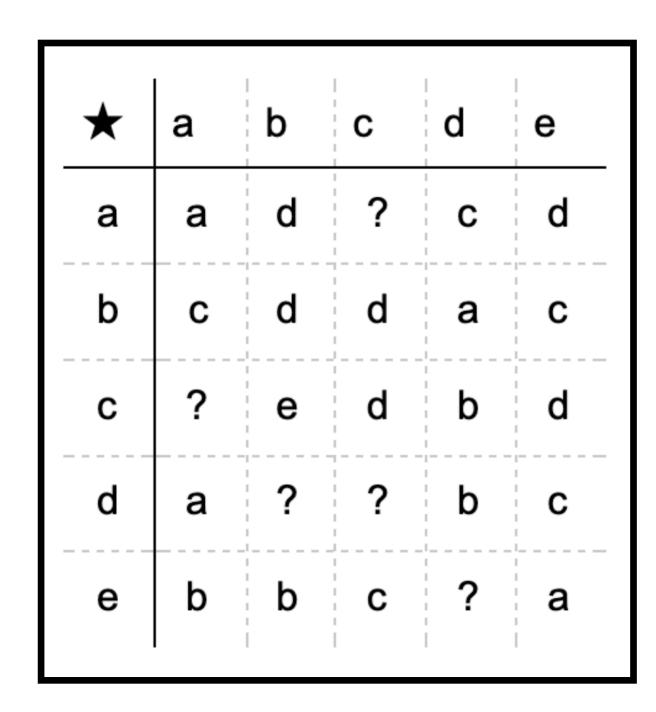
Reverse reasoning and verification Mathematical content produced by humans often presents a conclusion before outlining the reasoning that led to it. For example, the sentences "we will show next that x = 0 is a solution ..." or "We are going to prove the claim: AC is perpendicular to BD" can appear in a math problem's solution. This stylistic choice can improve readability, but it poses a challenge for natural language generation models, as it requires the model to infer the answer before producing the reasoning steps. We observe that not only does GPT-4 adopt this style, but it has an additional related drawback: even when it infers a clearly wrong answer at the start, it will still attempt to create justifications for it, instead of correcting it. This may again be due to the style of the training data, which mostly contains straightforwards solutions rather than trial-and-error style discussions and it is not clear whether or not it can be mitigated through a reinforcement learning phase (such as GPT-Instruct).

When/Why are Al capable/incapable?

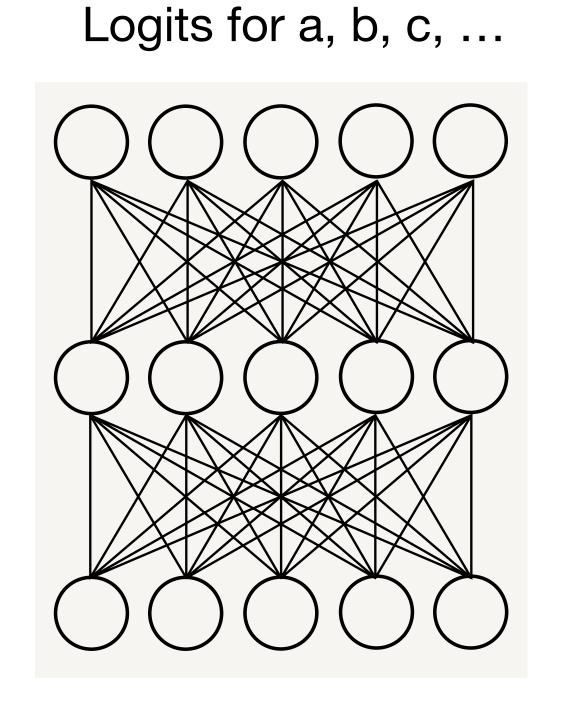
How do NN learn math (Grokking)

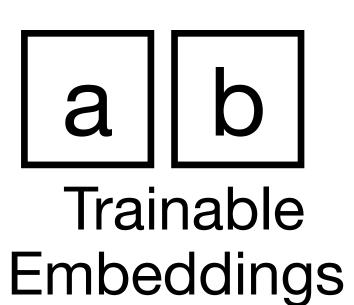
Train a neural network to learn binary operations

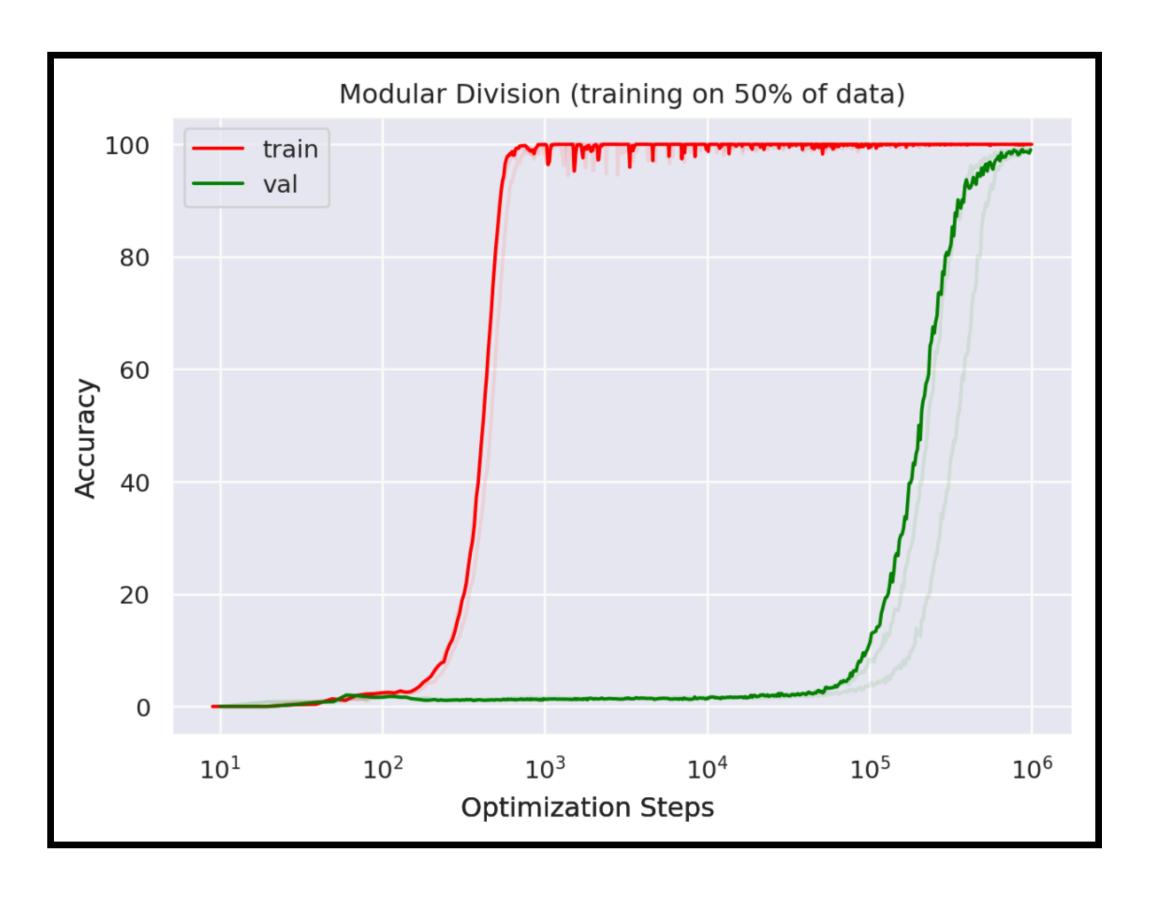
Phase transition behavior



$$a \circ b = c$$

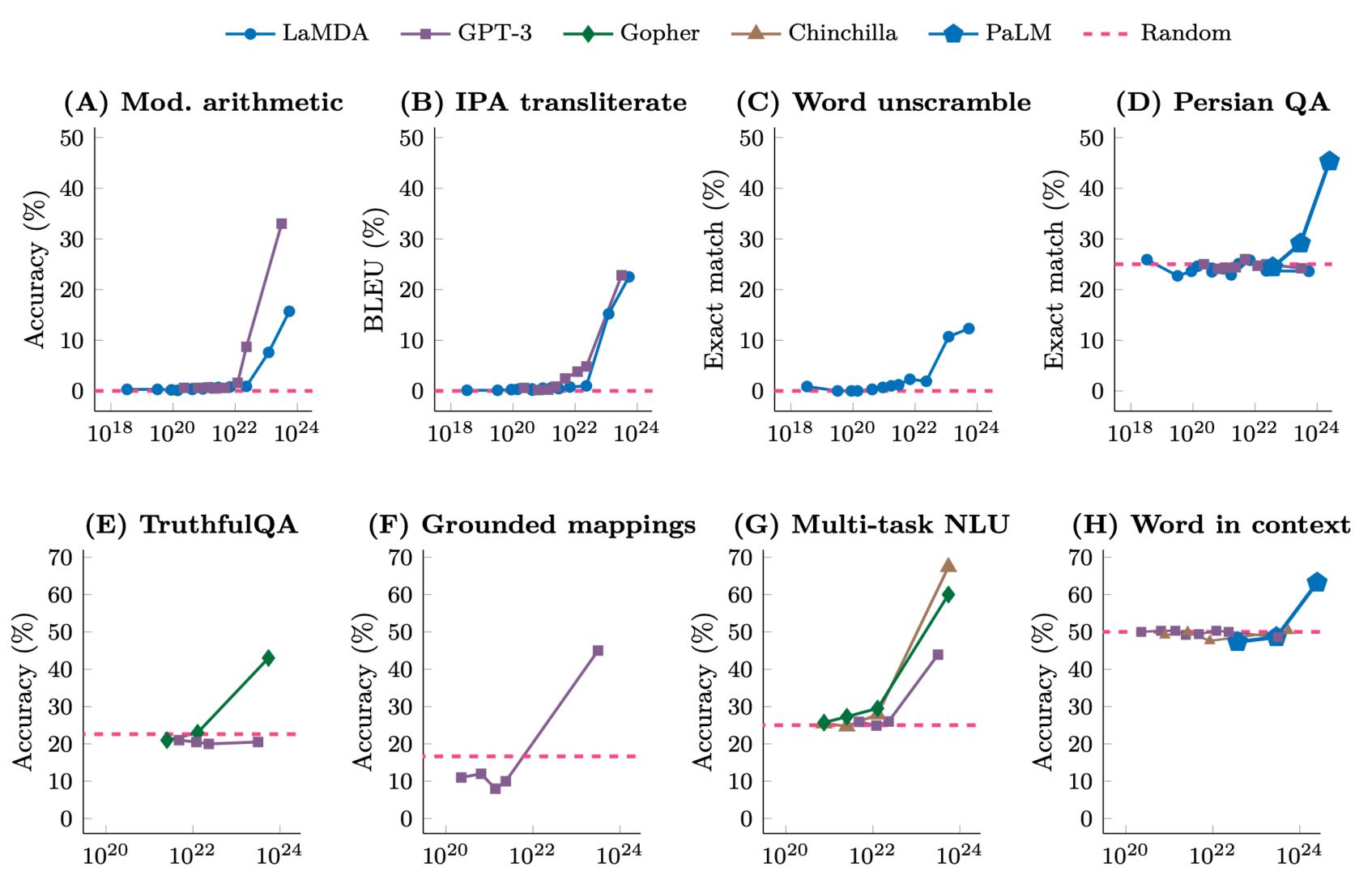






Grokking: Generalisation beyond overfitting on small algorithmic datasets 2201.02177

Emergent abilities (EA)

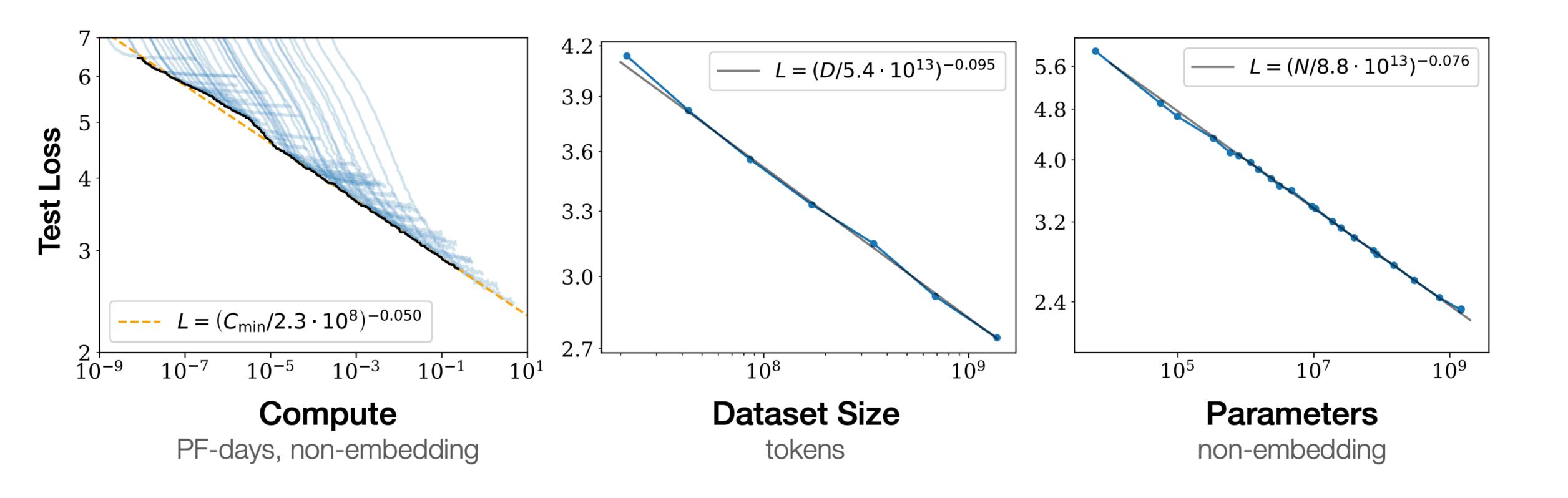


Model scale (training FLOPs)

Emergent Abilities of Large Language Models

arXiv: 2206.07682

Neural Scaling Laws (NSL)



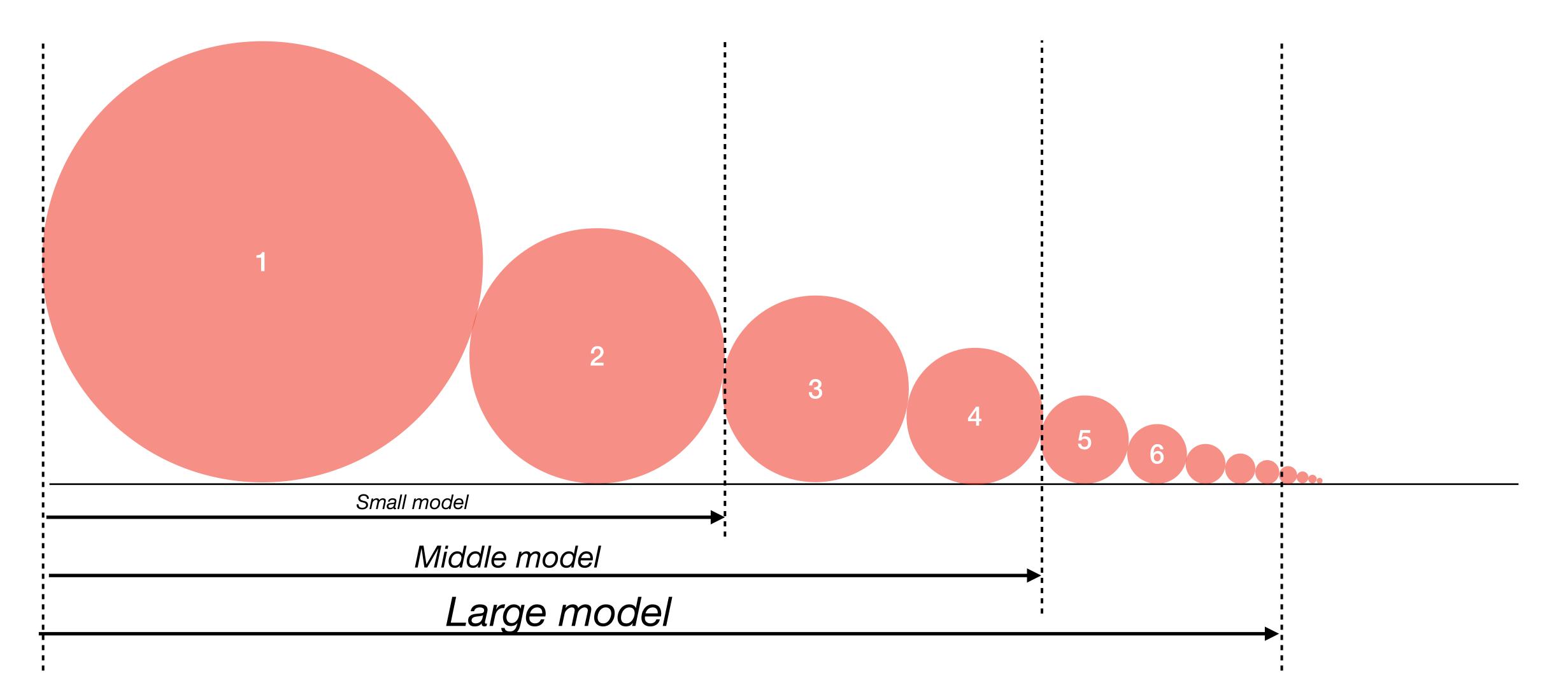
Scaling Laws for Neural Language Models, arXiv: 2001.08361

How EA leads to NSL

The quantisation model of neural scaling, arXiv: 2303.13506

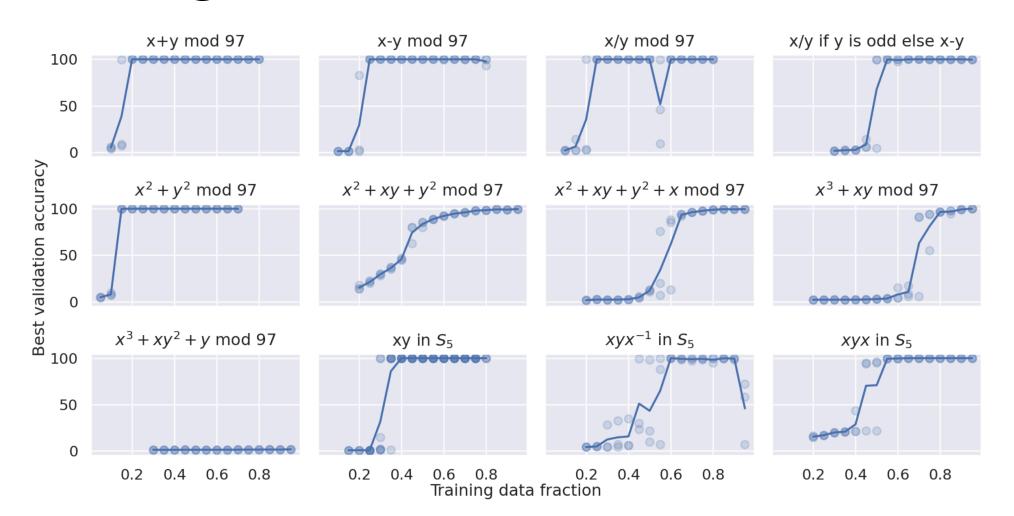
Knowledge quanta sequence

circle size = importance = frequency



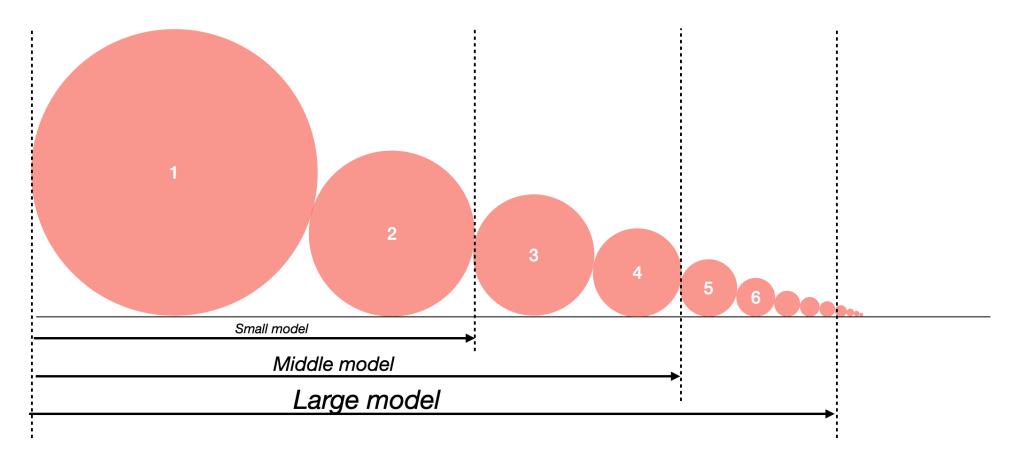
When are Al capable?

Enough data

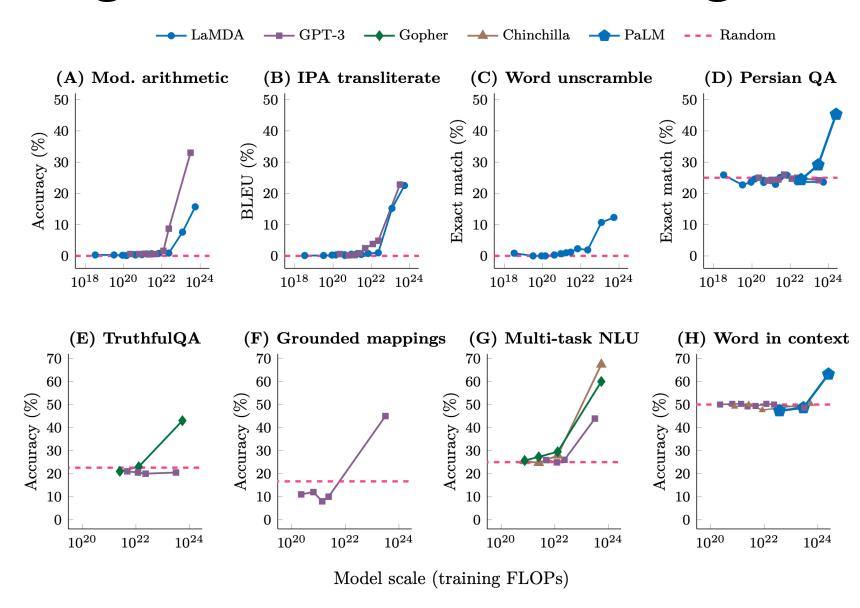


Pattern frequent enough

Knowledge quanta sequence



Enough model size, enough compute



Grokking: Generalisation beyond overfitting on small algorithmic datasets arXiv: 2201.02177

Emergent Abilities of Large Language Models

arXiv: 2206.07682

The quantisation model of neural scaling

arXiv: 2303.13506

Good news for human scientists

Enough data

Enough model size, enough compute

There are research areas which do not have much data, where model-driven is better than data-driven.

A problem may be too complicated for a blackbox Al to solve, but it may present simple structures humans can identify.

Pattern frequent enough

Precision vs Fuzziness

「数学天才」陶哲轩: GPT-4无 法攻克一个未解决的数学问题, 但对工作有帮助

新智元 新智元 2023-04-09 00:12

Arguably, the job of scientists is to forget about "common sense", in search of "outliers".

Science = Exploring "rare" events

Human languages are fuzzy, but math/physics are precise. The way human beings formulate ideas is fuzzy.



Humanity: Camps and survival strategies

Human scientists' attitudes towards Al

- The Survivors (幸存派) : admit AI has limitations, but reject AI. Humans can work in areas where AI has limitations.
- The Collaborators (合作派): admit AI has limitations, and accept AI. Only collaboration between AI and humans can lead to faster scientific development.
- The Redemptionists (拯救派): admit AI has limitations, and improve AI. Use scientific tools to develop better AI.
- The Self-rescuers (自救派): concern about AI safety. Humans need to focus on AI safety so that we can better understand and finally control AI.
- The worshipers (崇拜派): Al is omnipotent, and embrace Al. Humans needn't and cannot understand Al. Just take advantage of Al power.
- The Adventists (降临派): Al is omnipotent, embrace Al and become Al. Align human values to Al, not the other way around.

Disclaimer: Opinions are my own, which could be highly speculative. Some of these beliefs are quite extreme. Most people lie on the continuous spectrum rather than extreme points.

Survival strategies

- The Survivors (幸存派) : admit AI has limitations, but reject AI. Humans can work in areas where AI has limitations. Do research areas that AI cannot solve.
- The Collaborators (合作派): admit AI has limitations, and accept AI. Only collaboration between AI and humans can lead to faster scientific development. Find research areas that neither AI nor human can solve.
- The Redemptionists (拯救派): admit AI has limitations, and improve AI. Use scientific tools to develop better AI.
- The Self-rescuers (自救派): concern about AI safety. Humans need to focus on AI safety so that we can better understand and finally control AI. Research on AI interpretability.
- The worshipers (崇拜派): Al is omnipotent, and embrace Al. Humans needn't and cannot understand Al. Just take advantage of Al power.
- The Adventists (降临派): Al is omnipotent, embrace Al and become Al. Align human values to Al, not the other way around. I don't know...

Note: Some of these beliefs are quite extreme. Most people lie on the continuous spectrum rather than extreme points.

My Attitudes and Quest

- Collaborate, Rescue and self-rescue
- Collaborate with Al to speed up scientific discoveries
 - Example: Discovery of conserved quantities
- Rescue (improve) Al by leveraging tools developed in science
 - Example: Physics-inspired generative models
- Self-Rescue by research on Al interpretability/understanding
 - Example: Phase transitions, quantisation and modularity in neural networks

My quest - Collaborate: Discovery of Conserved Quantities

Al Poincare (discovering conserved quantities)

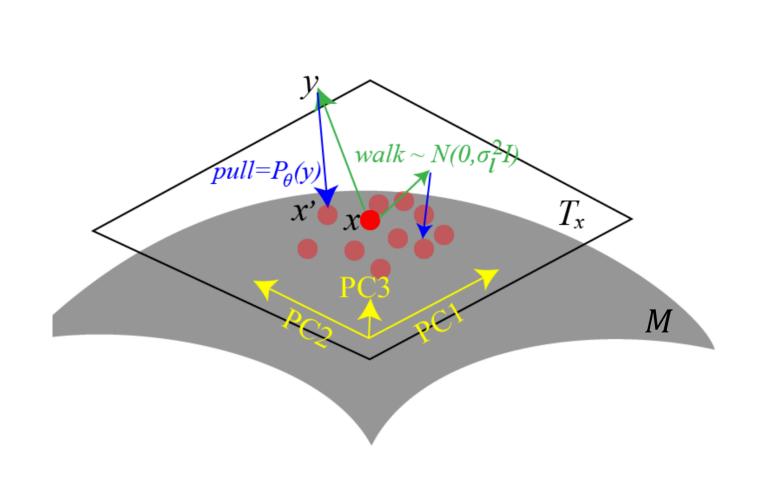
Data: trajectory

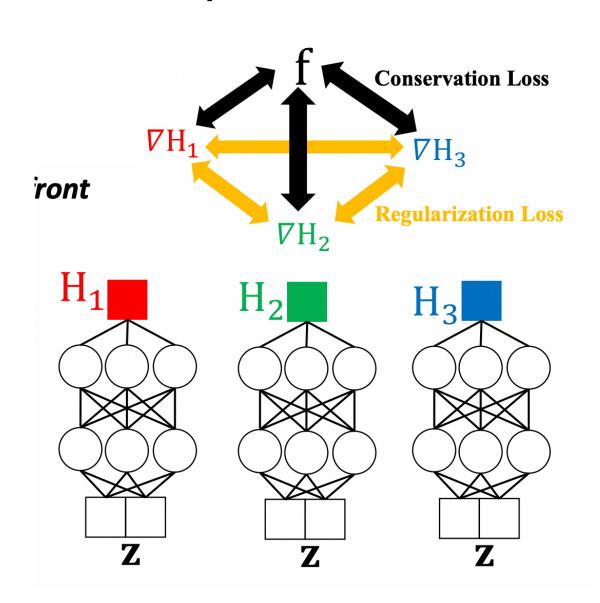
Assumption: No

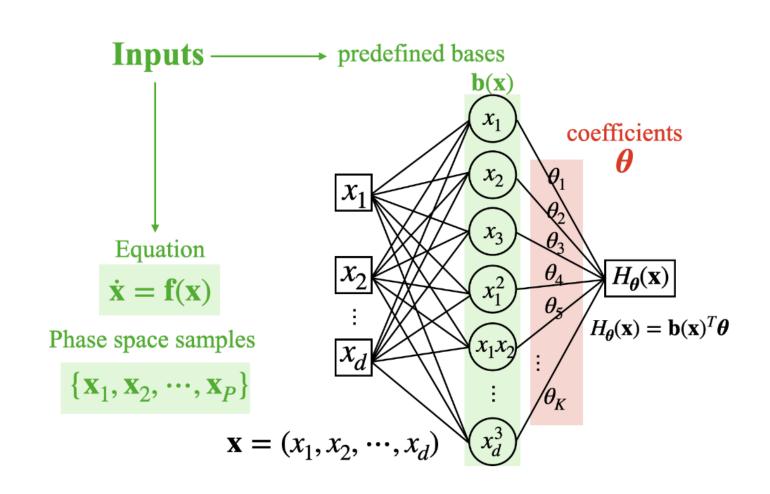
Data: differential equations

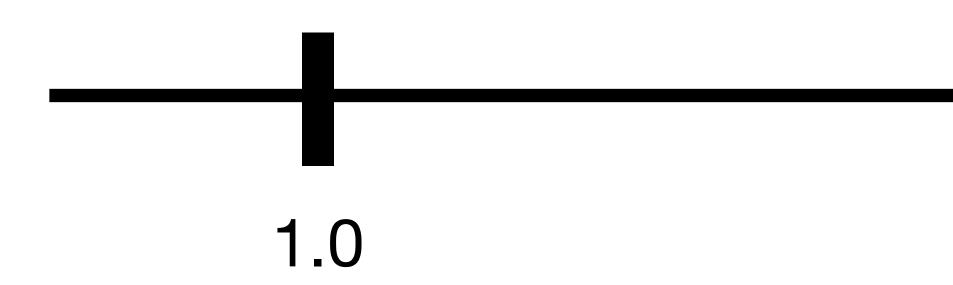
Assumption: No

Data: differential equations Assumption: basis functions





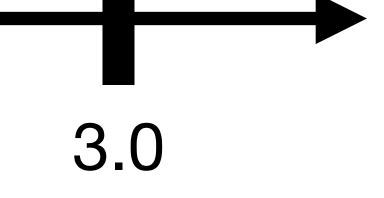




Phys. Rev. Lett. **126**, 180604

2.0

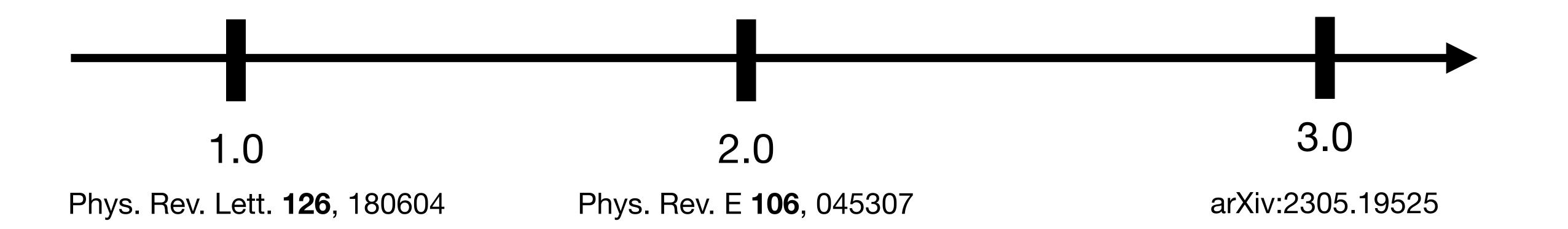
Phys. Rev. E 106, 045307



arXiv:2305.19525

Al Poincare: less is more

Data: trajectory Assumption: No	Data: differential equations Assumption: No	Data: differential equations Assumption: basis functions
1.0: A challenging setup	2.0: A simpler setup	3.0: An even simpler setup
Not interpretable	Reasonably interpretable	Extremely interpretable
Cannot discover unknown conserved quantities	Cannot discover unknown conserved quantities	Discover unknown conserved quantities!!!



Al Poincare 3.0 is not trivial!

Differential equations

```
The derivation of equations of motion is similar to 2D, only with area switched to volume. The phase space is 24D:
\mathbf{x} = (x_i, y_i, z_i, u_i, v_i, w_i), i = 1, 2, 3, 4. We list the equations here:
```

```
\dot{x_1} = u_1, \dot{u_1} = \lambda(-y_2z_3 + y_2z_4 + y_3z_2 - y_3z_4 - y_4z_2 + y_4z_3),
\dot{y_1} = v_1, \dot{v_1} = \lambda(x_2z_3 - x_2z_4 - x_3z_2 + x_3z_4 + x_4z_2 - x_4z_3),
\dot{z_1} = w_1, \dot{w_1} = \lambda(-x_2y_3 + x_2y_4 + x_3y_2 - x_3y_4 - x_4y_2 + x_4y_3),
\dot{x_2} = u_2, \dot{u_2} = \lambda(y_1z_3 - y_1z_4 - y_3z_1 + y_3z_4 + y_4z_1 - y_4z_3),
\dot{y_2} = v_2, \dot{v_2} = \lambda(-x_1z_3 + x_1z_4 + x_3z_1 - x_3z_4 - x_4z_1 + x_4z_3),
\dot{z}_2 = w_2, \dot{w}_2 = \lambda(x_1y_3 - x_1y_4 - x_3y_1 + x_3y_4 + x_4y_1 - x_4y_3),
                                                                                                                                  (C6)
\dot{x_3} = u_3, \dot{u_3} = \lambda(-y_1z_2 + y_1z_4 + y_2z_1 - y_2z_4 - y_4z_1 + y_4z_2),
\dot{y}_3 = v_3, \dot{v}_3 = \lambda(x_1z_2 - x_1z_4 - x_2z_1 + x_2z_4 + x_4z_1 - x_4z_2),
\dot{z}_3 = w_3, \dot{w}_3 = \lambda(-x_1y_2 + x_1y_4 + x_2y_1 - x_2y_4 - x_4y_1 + x_4y_2),
\dot{x_4} = u_4, \dot{u_4} = \lambda \cdot (y_1 z_2 - y_1 z_3 - y_2 z_1 + y_2 z_3 + y_3 z_1 - y_3 z_2),
\dot{y_4} = v_4, \dot{v_4} = \lambda(-x_1z_2 + x_1z_3 + x_2z_1 - x_2z_3 - x_3z_1 + x_3z_2),
\dot{z}_4 = w_4, \dot{w}_4 = \lambda(x_1y_2 - x_1y_3 - x_2y_1 + x_2y_3 + x_3y_1 - x_3y_2),
```

where

```
p = x_1(-v_2w_3 + v_2w_4 + v_3w_2 - v_3w_4 - v_4w_2 + v_4w_3) + y_1(u_2w_3 - u_2w_4 - u_3w_2 + u_3w_4 + u_4w_2 - u_4w_3)
    +z_1(-u_2v_3+u_2v_4+u_3v_2-u_3v_4-u_4v_2+u_4v_3)+x_2(v_1w_3-v_1w_4-v_3w_1+v_3w_4+v_4w_1-v_4w_3)
    +y_2(-u_1w_3+u_1w_4+u_3w_1-u_3w_4-u_4w_1+u_4w_3)+z_2(u_1v_3-u_1v_4-u_3v_1+u_3v_4+u_4v_1-u_4v_3)
    +x_3(-v_1w_2+v_1w_4+v_2w_1-v_2w_4-v_4w_1+v_4w_2)+y_3(u_1w_2-u_1w_4-u_2w_1+u_2w_4+u_4w_1-u_4w_2)
    +z_3(-u_1v_2+u_1v_4+u_2v_1-u_2v_4-u_4v_1+u_4v_2)+x_4(v_1w_2-v_1w_3-v_2w_1+v_2w_3+v_3w_1-v_3w_2)
    + y_4(-u_1w_2 + u_1w_3 + u_2w_1 - u_2w_3 - u_3w_1 + u_3w_2) + z_4(u_1v_2 - u_1v_3 - u_2v_1 + u_2v_3 + u_3v_1 - u_3v_2)
q = (-y_2z_3 + y_2z_4 + y_3z_2 - y_3z_4 - y_4z_2 + y_4z_3)^2 + (x_2z_3 - x_2z_4 - x_3z_2 + x_3z_4 + x_4z_2 - x_4z_3)^2
    +\left(-x_2y_3+x_2y_4+x_3y_2-x_3y_4-x_4y_2+x_4y_3\right)^2+\left(y_1z_3-y_1z_4-y_3z_1+y_3z_4+y_4z_1-y_4z_3\right)^2
    +(-x_1z_3+x_1z_4+x_3z_1-x_3z_4-x_4z_1+x_4z_3)^2+(x_1y_3-x_1y_4-x_3y_1+x_3y_4+x_4y_1-x_4y_3)^2
    + \left(-y_1 z_2 + y_1 z_4 + y_2 z_1 - y_2 z_4 - y_4 z_1 + y_4 z_2\right)^2 + \left(x_1 z_2 - x_1 z_4 - x_2 z_1 + x_2 z_4 + x_4 z_1 - x_4 z_2\right)^2
    +\left(-x_{1}y_{2}+x_{1}y_{4}+x_{2}y_{1}-x_{2}y_{4}-x_{4}y_{1}+x_{4}y_{2}\right)^{2}+\left(y_{1}z_{2}-y_{1}z_{3}-y_{2}z_{1}+y_{2}z_{3}+y_{3}z_{1}-y_{3}z_{2}\right)^{2}
```

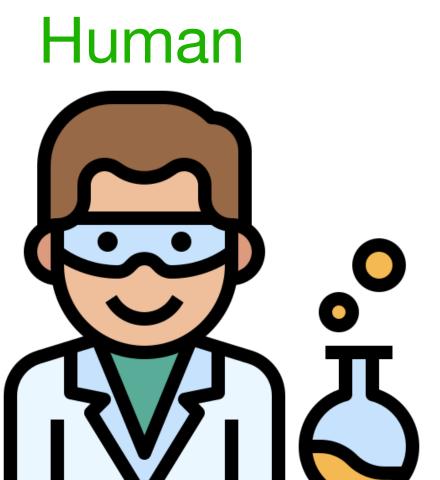
Constraints

 $+(-x_1z_2+x_1z_3+x_2z_1-x_2z_3-x_3z_1+x_3z_2)^2+(x_1y_2-x_1y_3-x_2y_1+x_2y_3+x_3y_1-x_3y_2)^2$

and with the constant-volume constraint

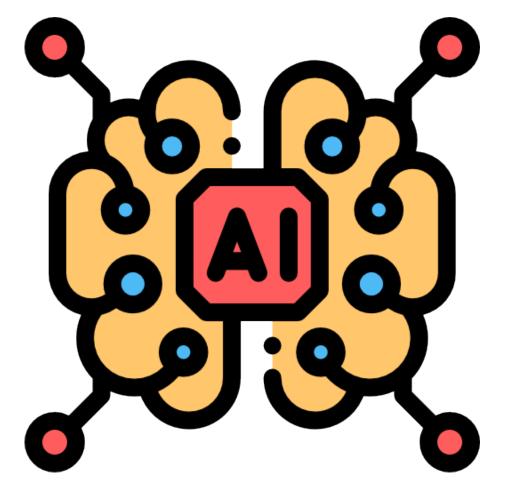
```
0 = (-y_2z_3 + y_2z_4 + y_3z_2 - y_3z_4 - y_4z_2 + y_4z_3)u_1 + (x_2z_3 - x_2z_4 - x_3z_2 + x_3z_4 + x_4z_2 - x_4z_3)v_1
     +(-x_2y_3+x_2y_4+x_3y_2-x_3y_4-x_4y_2+x_4y_3)w_1+(y_1z_3-y_1z_4-y_3z_1+y_3z_4+y_4z_1-y_4z_3)u_2
     +\left(-x_1z_3+x_1z_4+x_3z_1-x_3z_4-x_4z_1+x_4z_3\right)v_2+\left(x_1y_3-x_1y_4-x_3y_1+x_3y_4+x_4y_1-x_4y_3\right)w_2
                                                                                                                                      (C8)
     +\left(-y_1z_2+y_1z_4+y_2z_1-y_2z_4-y_4z_1+y_4z_2\right)u_3+\left(x_1z_2-x_1z_4-x_2z_1+x_2z_4+x_4z_1-x_4z_2\right)v_3
     +\left(-x_{1}y_{2}+x_{1}y_{4}+x_{2}y_{1}-x_{2}y_{4}-x_{4}y_{1}+x_{4}y_{2}\right)w_{3}+\left(y_{1}z_{2}-y_{1}z_{3}-y_{2}z_{1}+y_{2}z_{3}+y_{3}z_{1}-y_{3}z_{2}\right)u_{4}
     +\left(-x_1z_2+x_1z_3+x_2z_1-x_2z_3-x_3z_1+x_3z_2\right)v_4+\left(x_1y_2-x_1y_3-x_2y_1+x_2y_3+x_3y_1-x_3y_2\right)w_4
```

Question: How many conserved quantities do the differential equations have?



(Two months' hard work) I found 12!

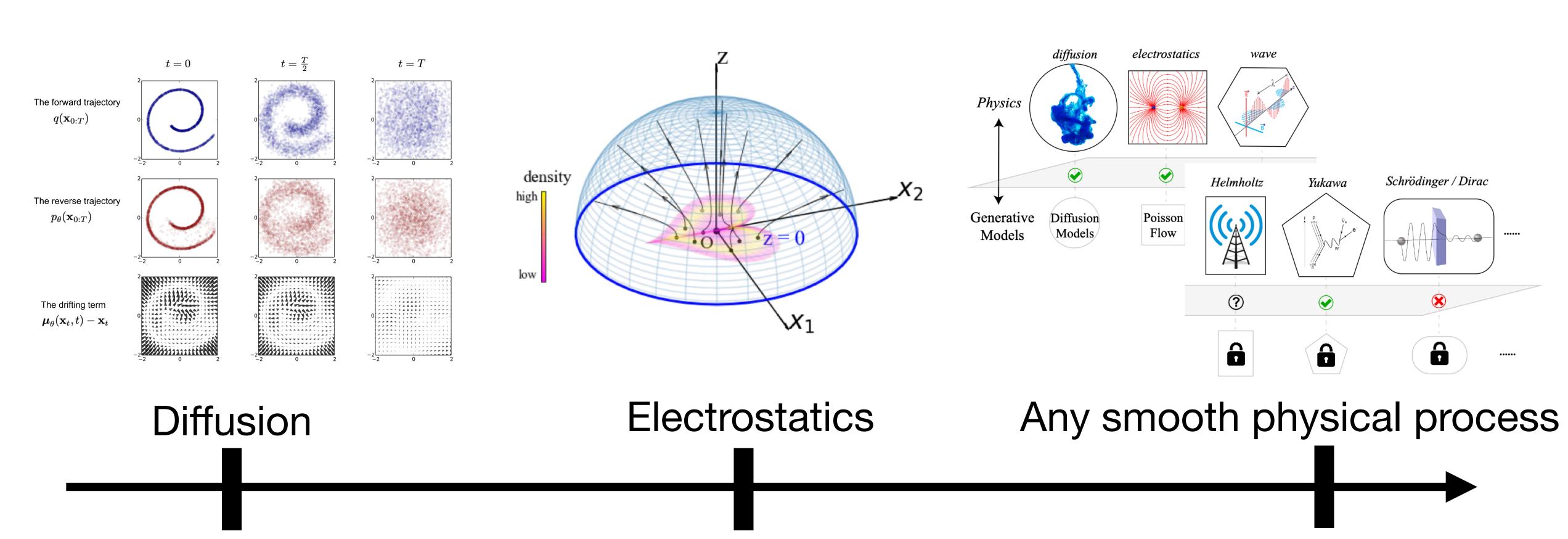
Al Poincare 3.0



(< 1 minute) I found 14!

My quest - **Rescue**: Physics-inspired generative models

Generative models from physical processes



Diffusion model (Not my work)

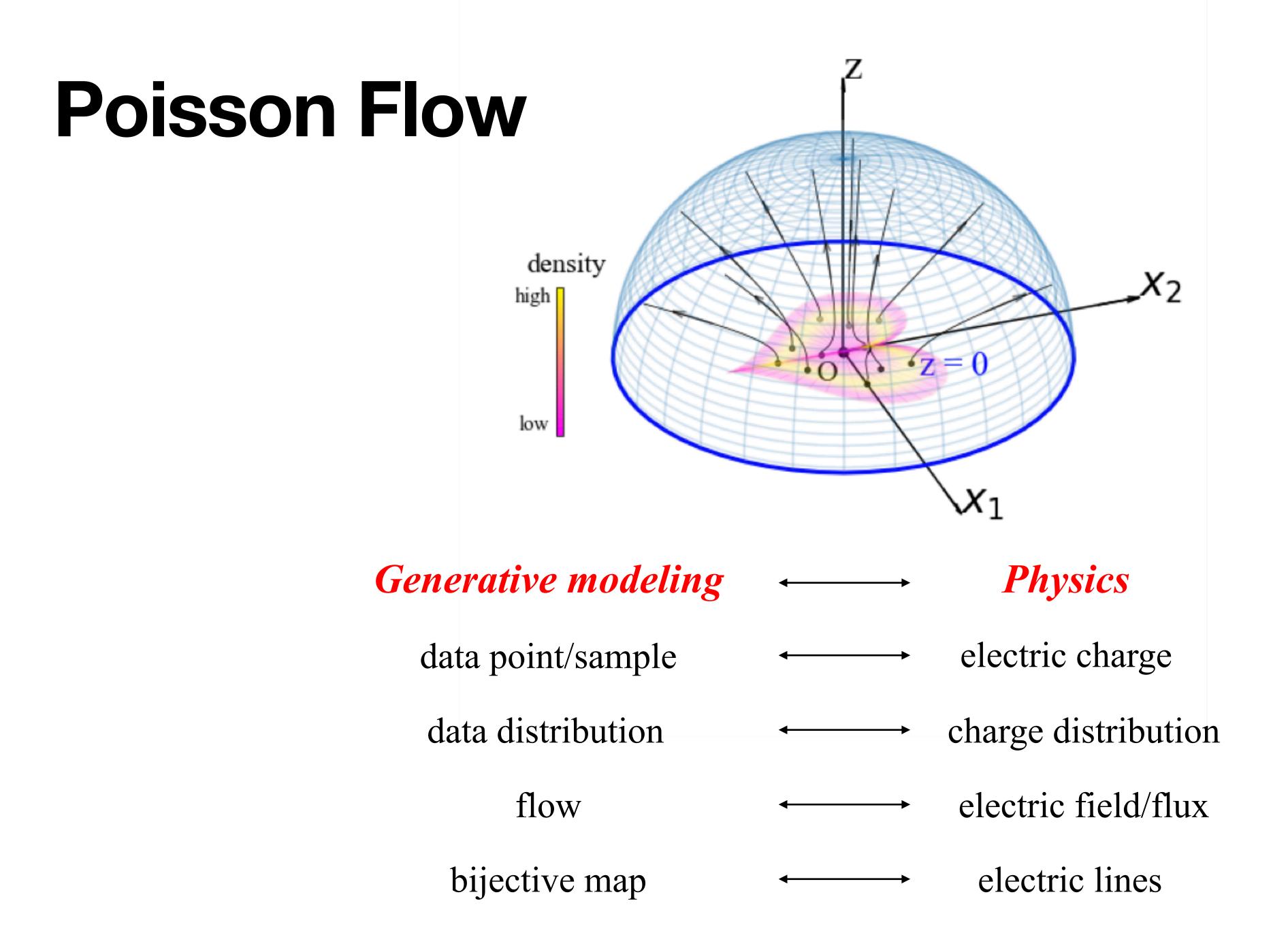
arXiv: 1503.03585

Poisson Flow

Poisson Flow Generative Models arXiv: 2209.11178 (NeurIPS 2022)

GenPhys

From Physical Processes to Generative Models arXiv: 2304.02637



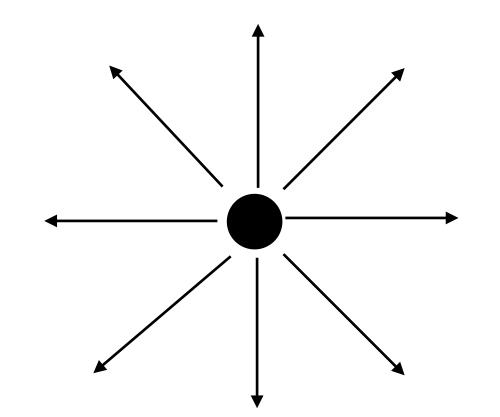
Electrostatics

Poisson Equation
$$\nabla^2 \varphi = -\rho(x), \ \nabla^2 \equiv \sum_{i=1}^{N} \partial_i^2$$

Green function

$$\nabla^2 G(x, x') = -\delta(x - x') \Longrightarrow G(x, x') \sim r^{-(N-2)}, r \equiv ||x - x'||$$

$$\varphi(x) = \int G(x, x') \rho(x') dx' \qquad E(x) = -\nabla \varphi(x) \sim \int \frac{x - x'}{||x - x'||^N} \rho(x') dx'$$



$$N = 3 \Longrightarrow \varphi(r) \sim \frac{1}{r}, E(r) \sim \frac{1}{r^2}$$

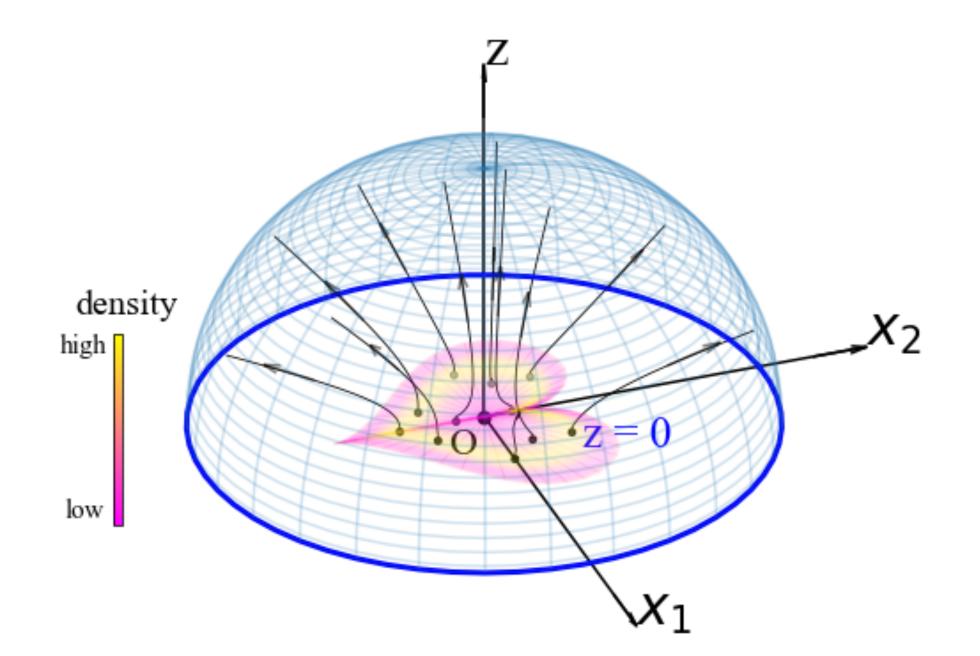
$$N \ge 3 \Longrightarrow \varphi(r) \sim \frac{1}{r^{N-2}}, E(r) \sim \frac{1}{r^{N-1}}$$

Electric field generalize

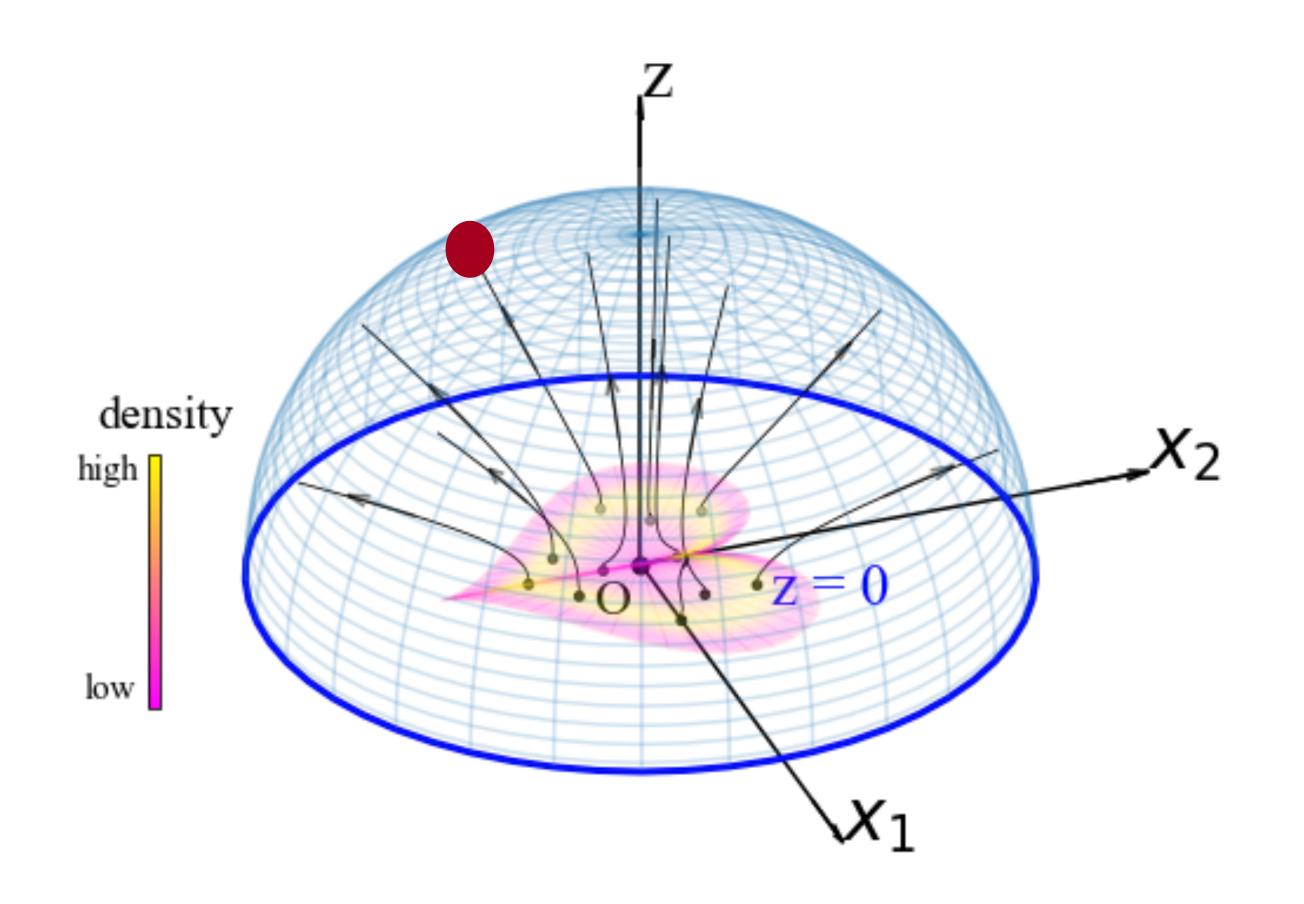
Poisson field

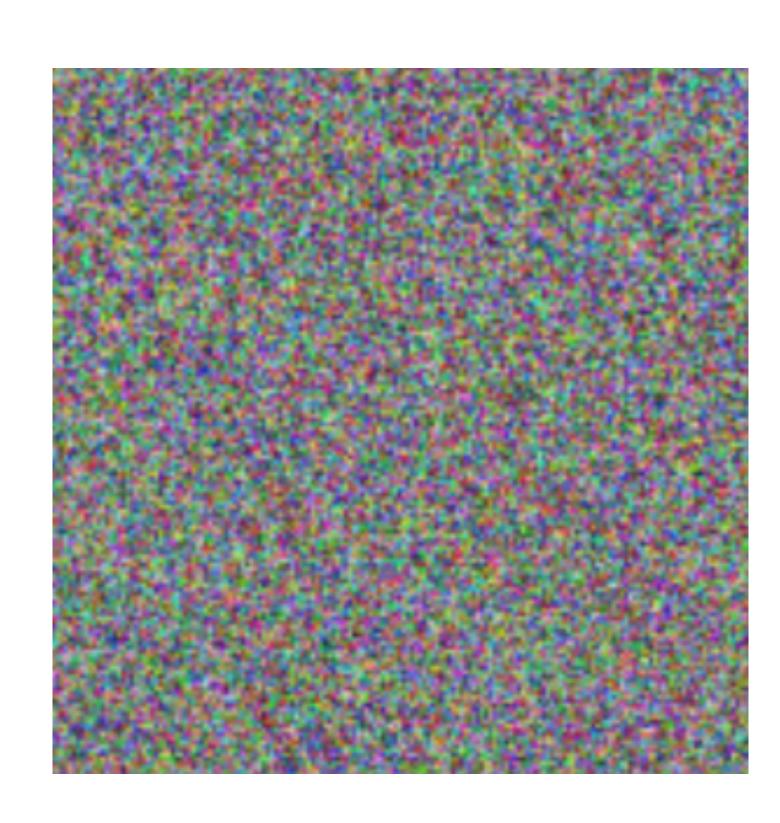
Poisson Flow: a New Flow Inspired by Electrostatics

- Interpret N-dim data distribution as charge density
- Placing the charges on the z = 0 hyperplane in an N + 1-dim space augmented with dimension z
- Electric Field Lines define a bijection between data distribution and a uniform distribution on the large hemisphere

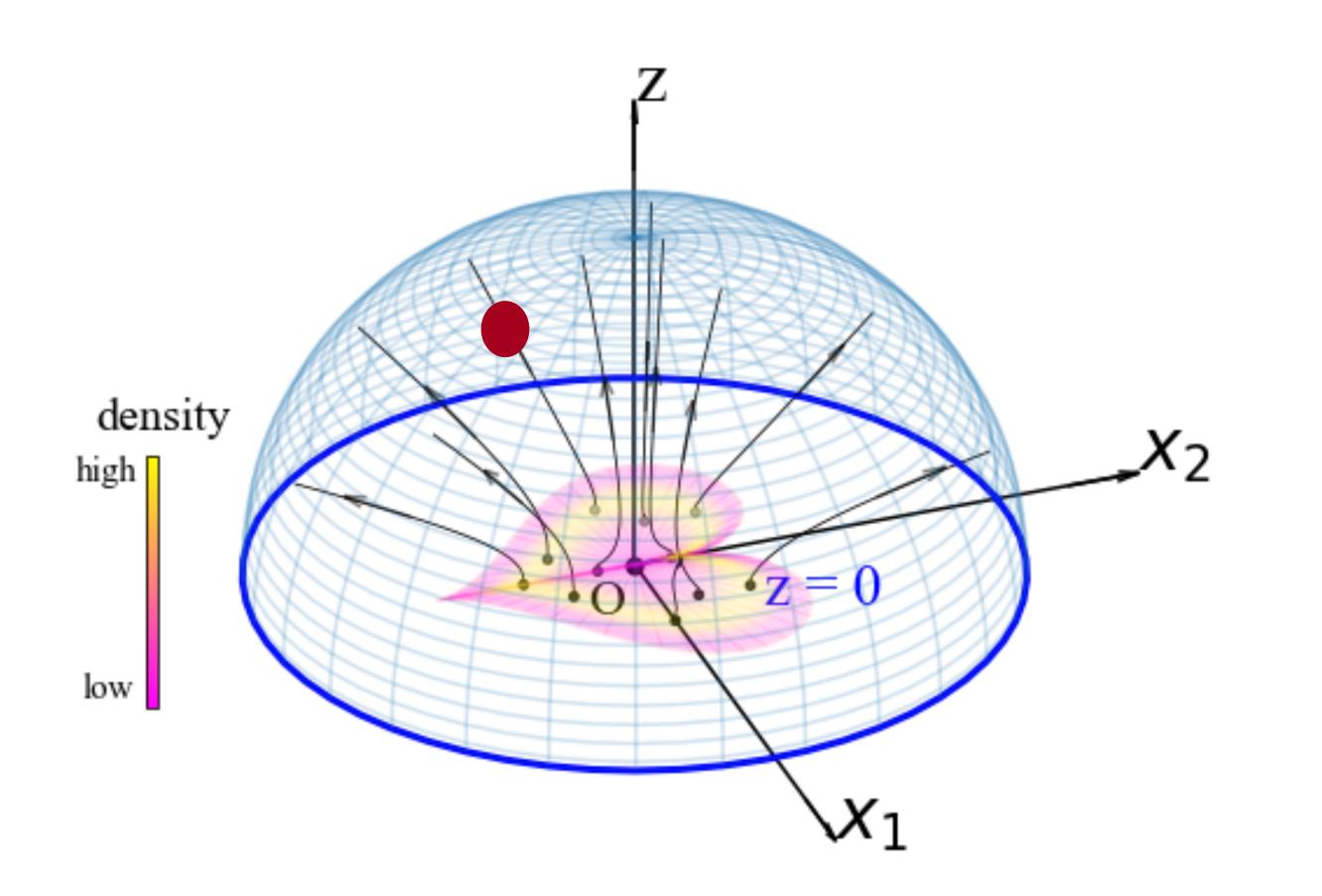


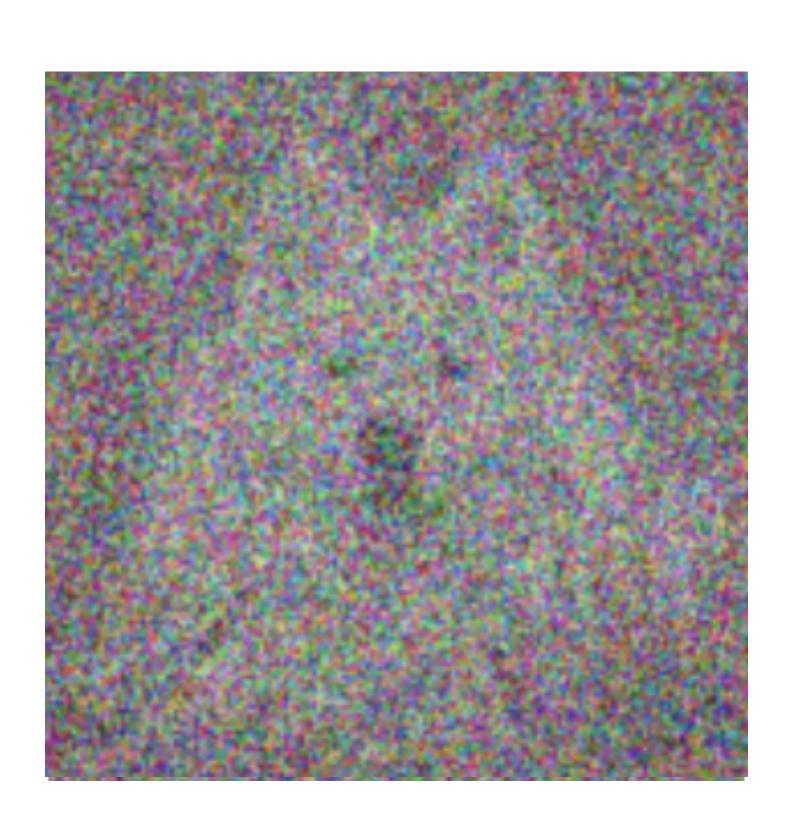
1. Uniformly sampling an initial sample () on the hemisphere.



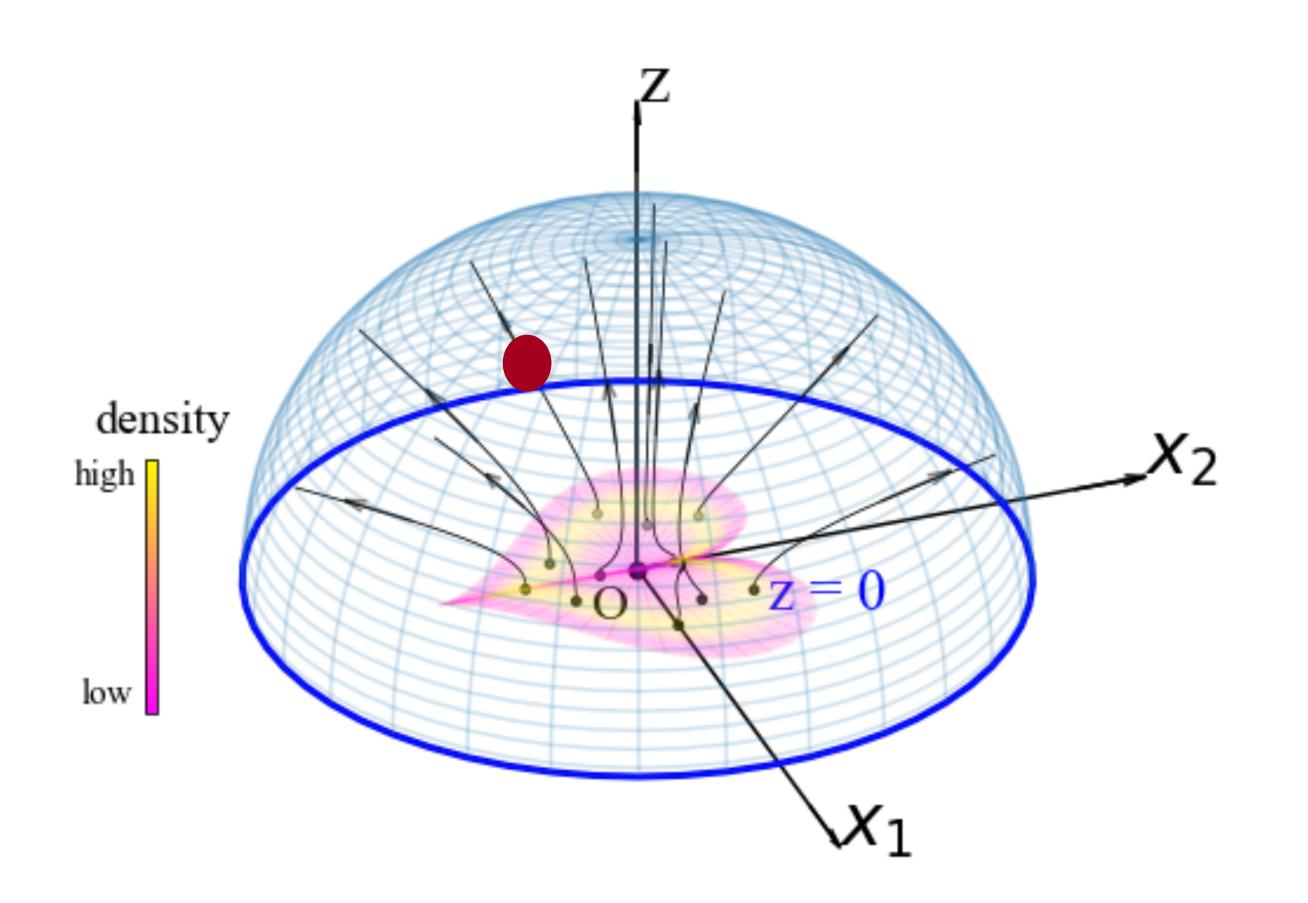


- 1. Uniformly sampling an initial sample () on the hemisphere.
- 2. Evolving the sample by following the corresponding electric field line.



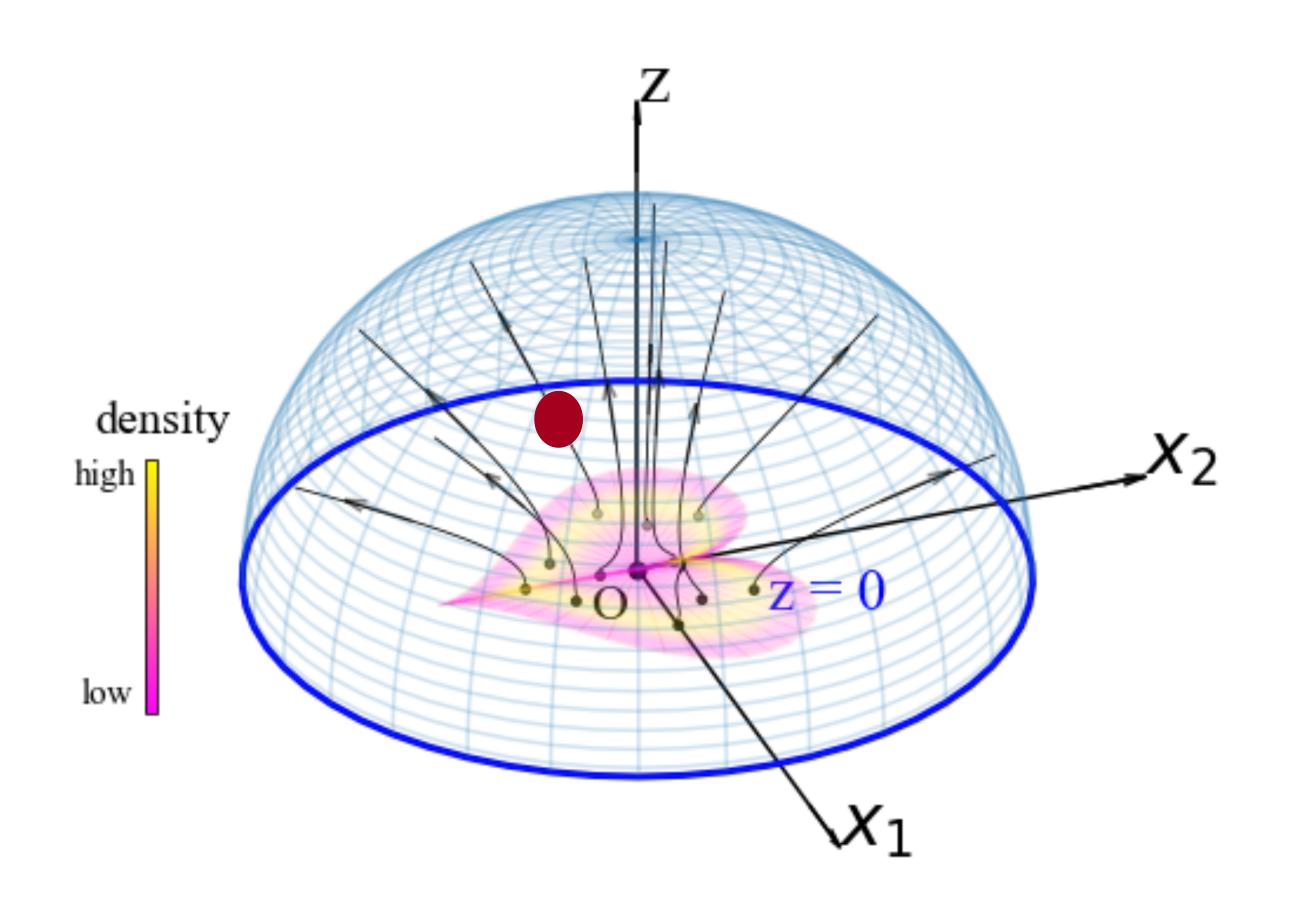


- 1. Uniformly sampling an initial sample () on the hemisphere.
- 2. Evolving the sample by following the corresponding electric field line.





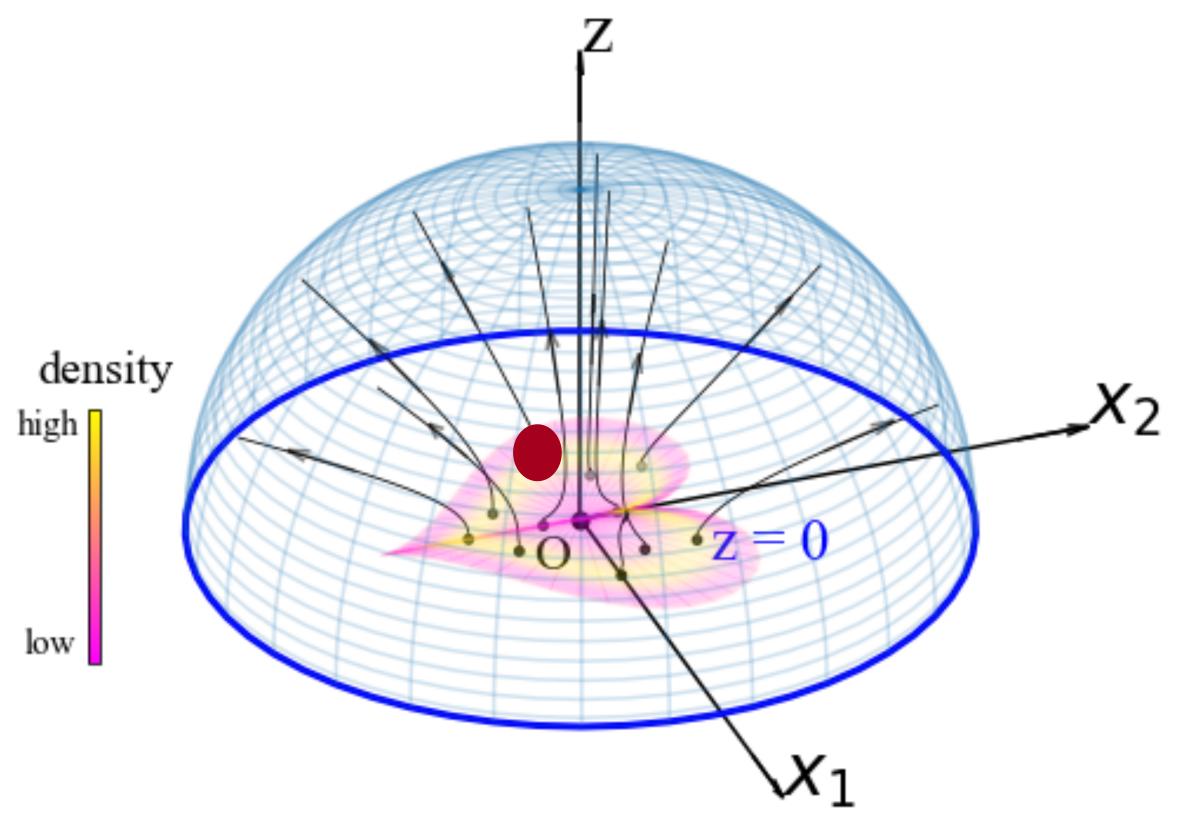
- 1. Uniformly sampling an initial sample () on the hemisphere.
- 2. Evolving the sample by following the corresponding electric field line.

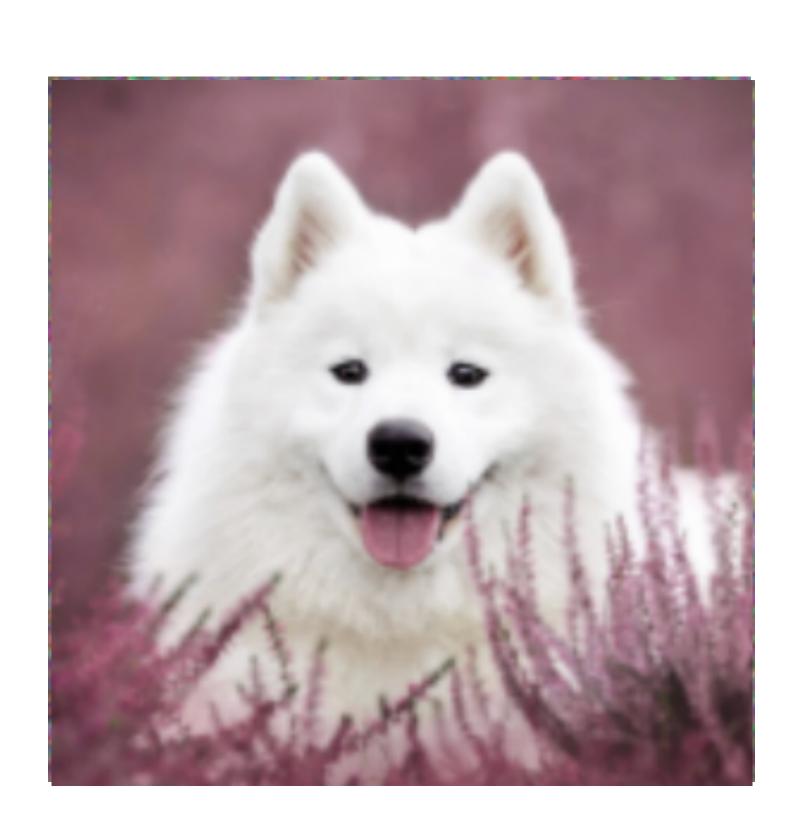




Generation

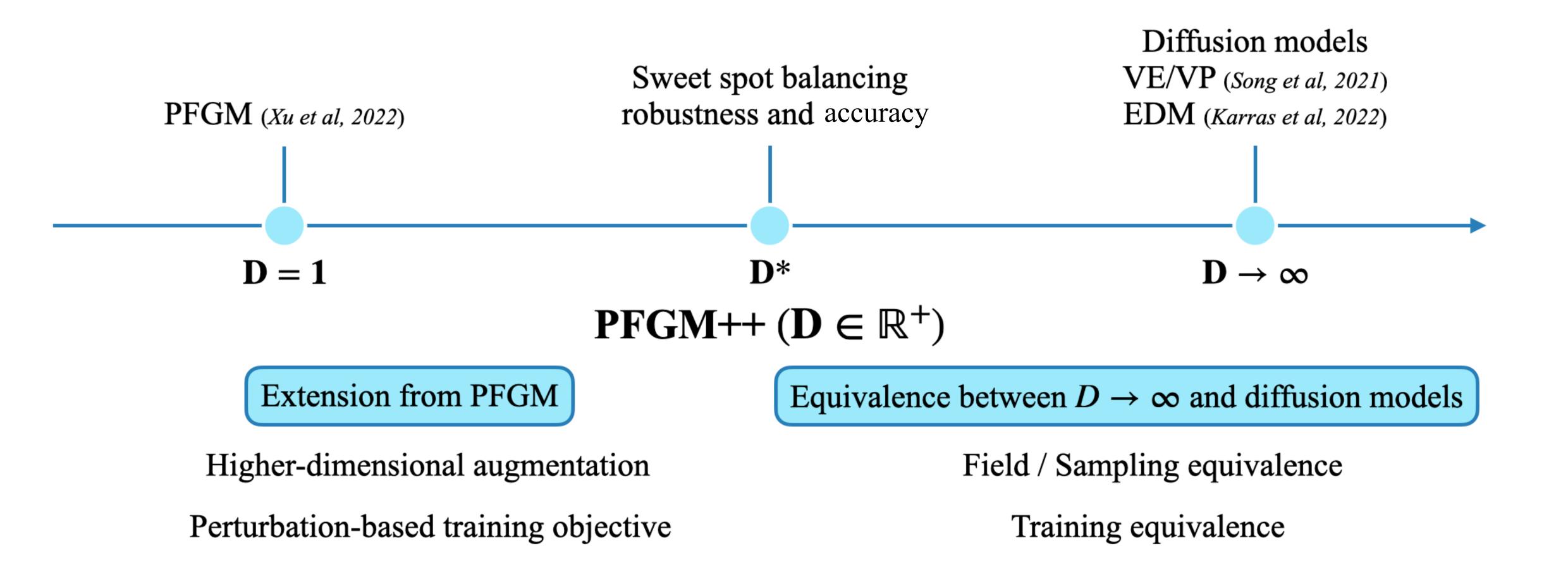
- 1. Uniformly sampling an initial sample () on the hemisphere.
- 2. Evolving the sample by following the corresponding electric field line.
- 3. Stopping the process when z = 0.





Q: Relation between Diffusion Models and Poisson Flows?

PFGM++ framework



Xu, Liu, Tong, Tian, Tegmark, and Jaakkola. PFGM++: Unlocking the Potential of Physics-Inspired Generative Models, arXiv: 2302.04265

Q: Is there a universal converter from physics to generative models?

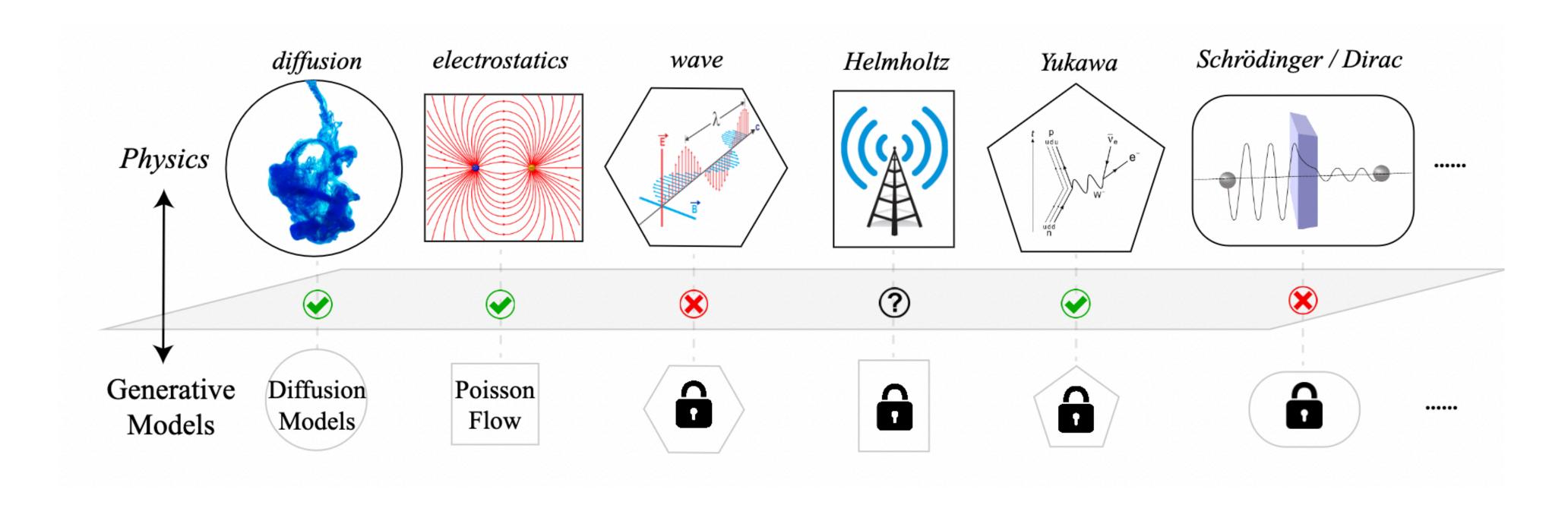
A: Yes, but...

GenPhys: From Physical Processes to Generative Models

arXiv: 2304.02637

Yes: A concrete protocol that converts physics to generative models

but: the converted generative models may not have desirable properties



Converter: partial differential equations (PDEs)

A physical process is described by a PDE

GenPhys: From Physical Processes to Generative Models arXiv: 2304.02637

$$\hat{L}\phi \equiv F(\phi, \phi_t, \phi_{tt}, \nabla \phi, \nabla^2 \phi, ...) = f(\mathbf{x}, t)$$
 (Physical PDE)

Physicists already know how to solve it, ...

..., if they are equivalent, ...

A generative model is associated with a density flow (which is also a PDE)

$$\hat{M}(p, \mathbf{v}, R) \equiv \frac{\partial p(\mathbf{x}, t)}{\partial t} + \nabla \cdot [p(\mathbf{x}, t)\mathbf{v}(\mathbf{x}, t)] - R(\mathbf{x}, t) = p_{\text{data}}(\mathbf{x})\delta(t) \quad \text{(Density Flow)}$$



..., then we know how to solve this one, too. By "solve", we mean a design of (p, v, R).

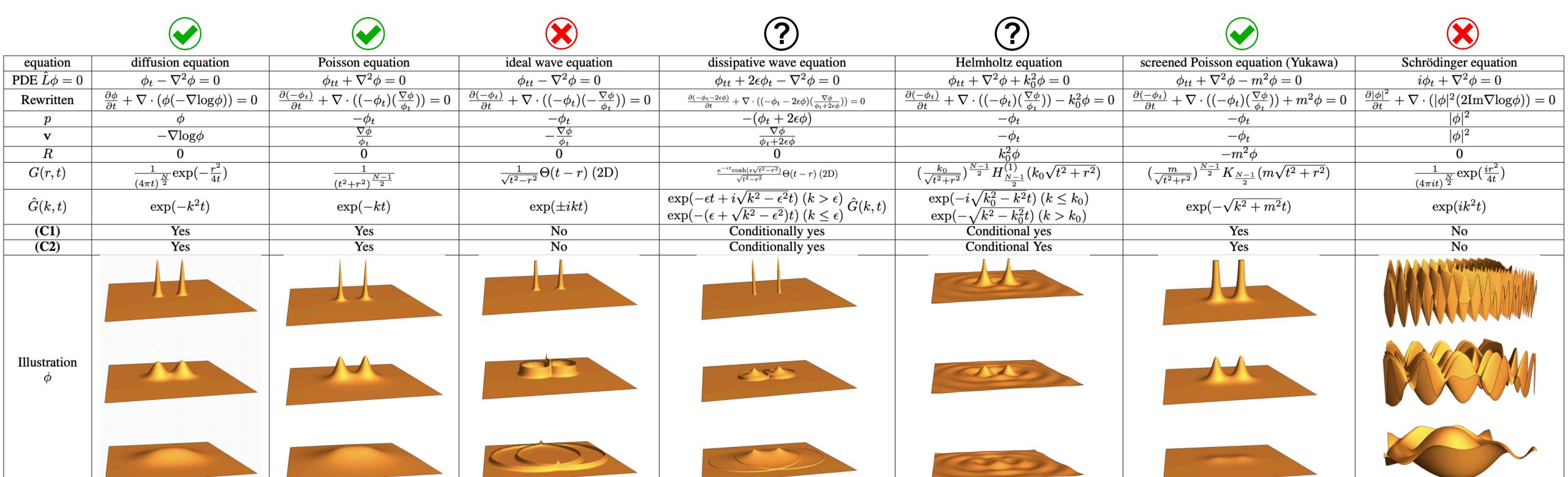
Examples

Yes (Diffusion Models)

s-generative?

Yes (Poisson Flow)

No



Conditionally Yes (large ϵ)

Conditionally yes (small k)

Yes

No

My quest - **Self-Rescue:** Al interpretability

(Phase transitions, quantisation, modularity)

8:07



"Let's offer \$100 billion in prizes for interpretability. Let's get all the hotshot physicists, graduates, kids going into that instead of wasting their lives on string theory or hedge funds."

"We are so far behind right now. The interpretability people are working on stuff smaller than GPT-2... We've got GPT-4 now. Let the \$100 billion in prizes be claimed for understanding GPT-4."

"As long as that hasn't happened, then that's like a fond dream of a pleasant world we could live in and not the world we actually live in right now."

- @ESYudkowsky

2:32 AM · 4/9/23 · 63.1K Views

25 Retweets 3 Quotes 238 Likes 36 Bookmarks

Tweet your reply





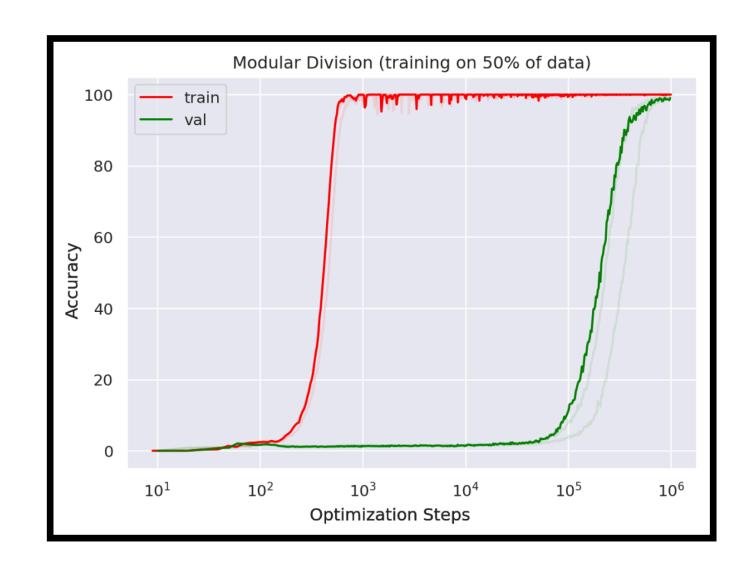






Physics of Al

Grokking (phase transitions)

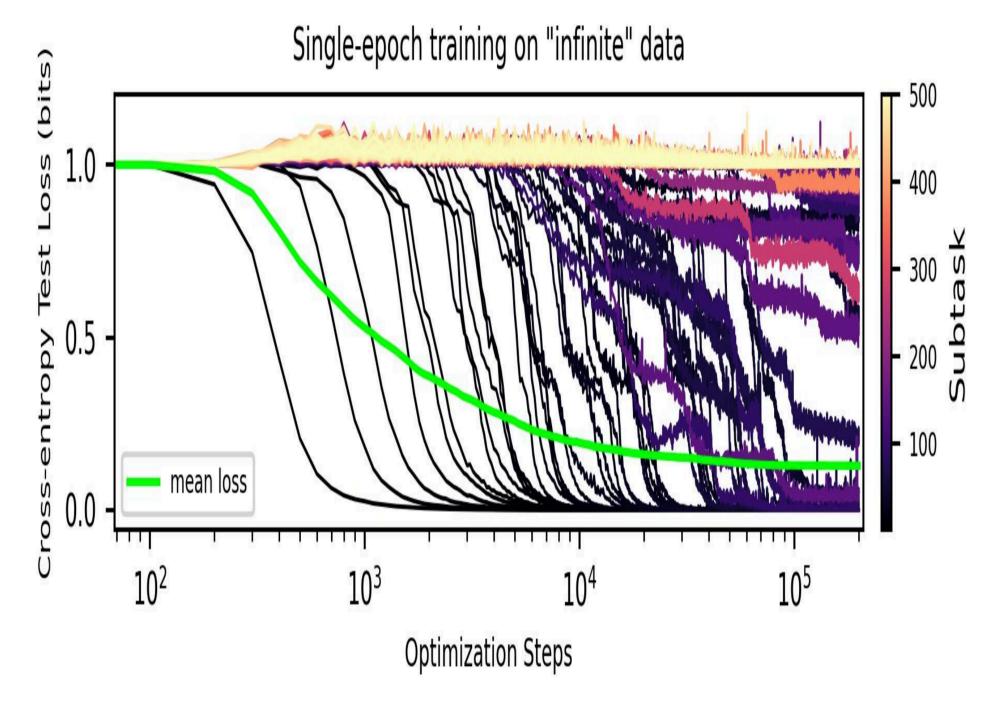


Towards understanding grokking: An effective theory of representation learning arXiv: 2205.10343 (NeurIPS 2022)

Omnigrok: Grokking Beyond Algorithmic data

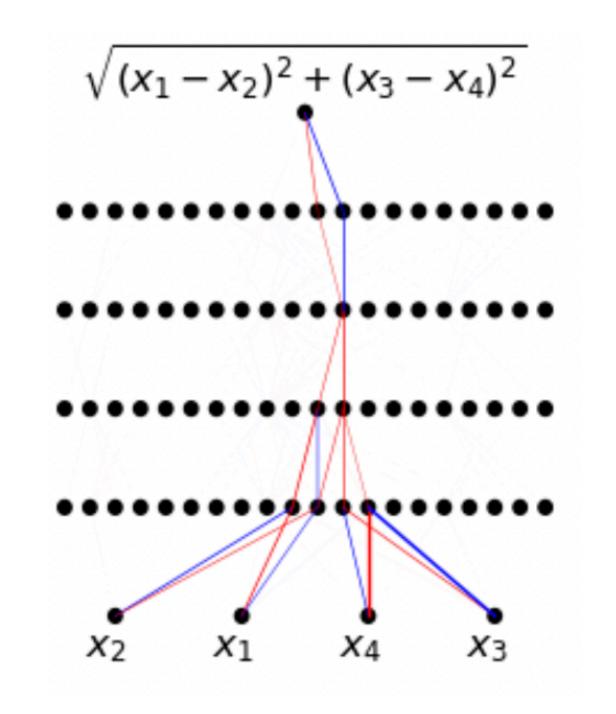
arXiv: 2210.01117 (ICLR 2023)

Quantization



A Quantization Model of Neural Scaling arXiv: 2303.13506

Locality/Modularity



"Seeing is Believing: Brain-Inspired Modular Training for Mechanistic Interpretability" https://arxiv.org/abs/2305.08746

Learning addition

Addition dataset

addition

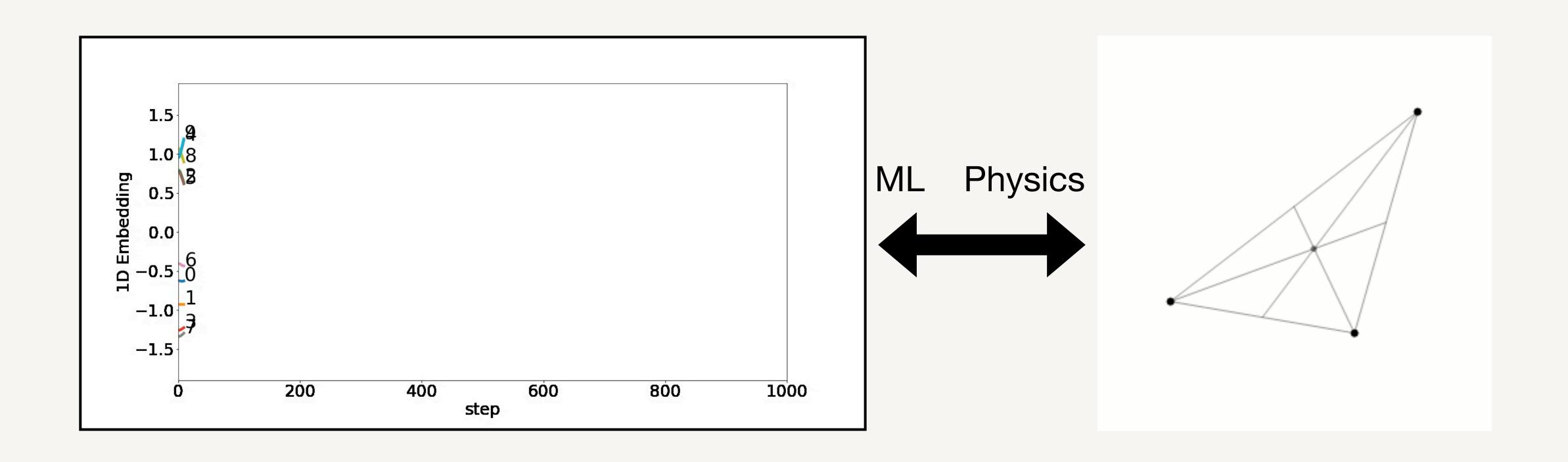
Predict 8

Towards understanding grokking: An effective theory of representation learning arXiv: 2205.10343 (NeurIPS 2022)

Fit the result MLP "Decoder" Operation

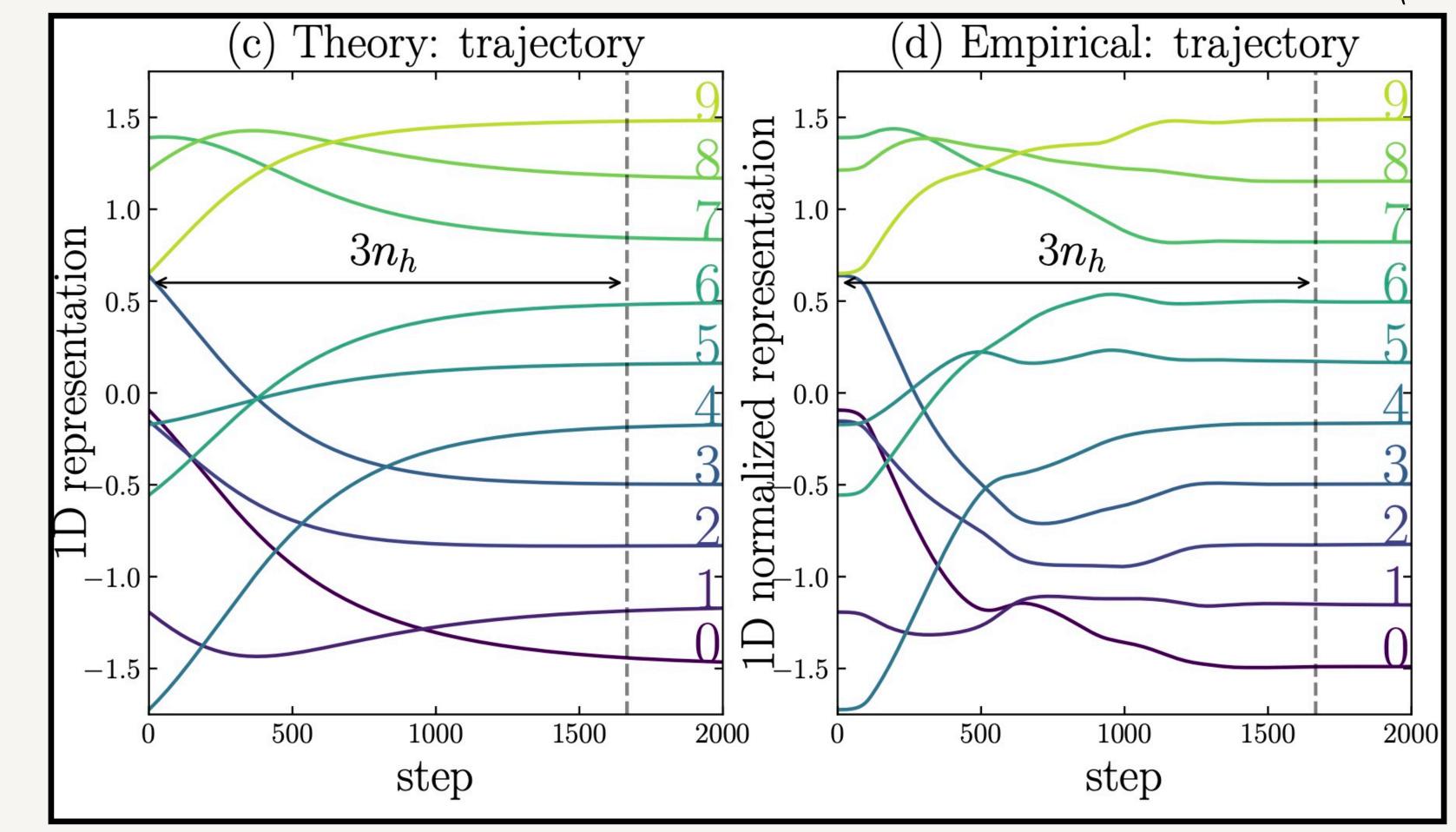
The dynamics of representation

Towards understanding grokking: An effective theory of representation learning arXiv: 2205.10343 (NeurIPS 2022)

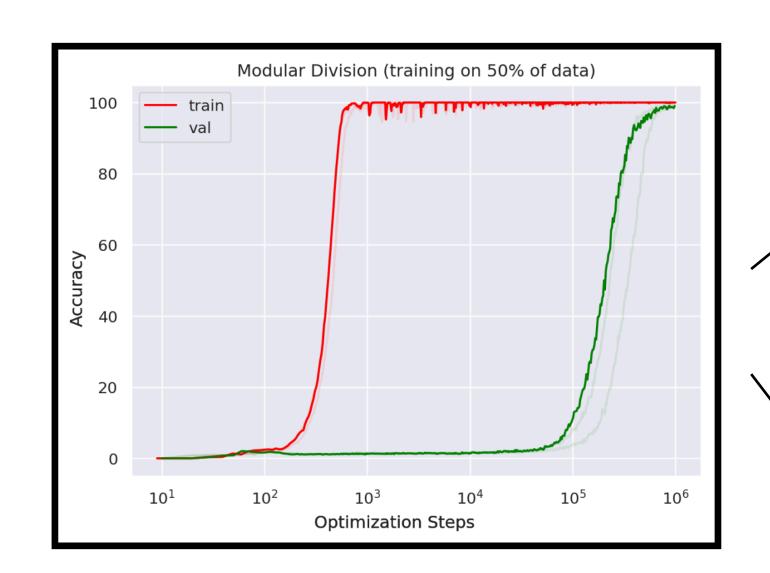


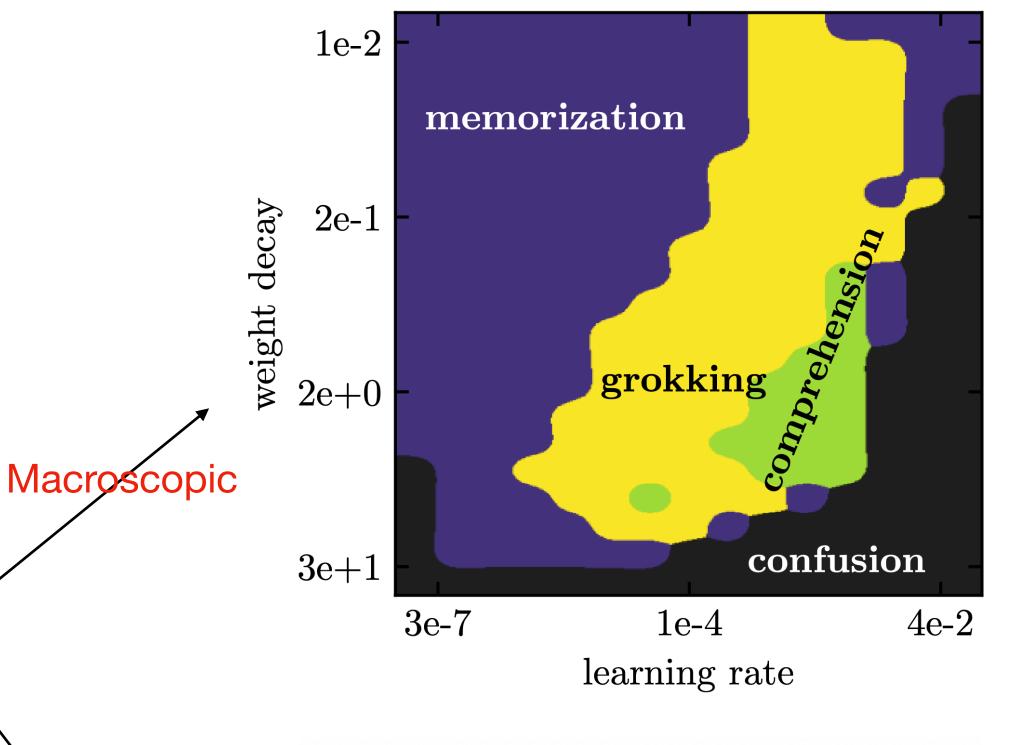
Compare theory and experiment

Towards understanding grokking: An effective theory of representation learning arXiv: 2205.10343 (NeurIPS 2022)



Grokking

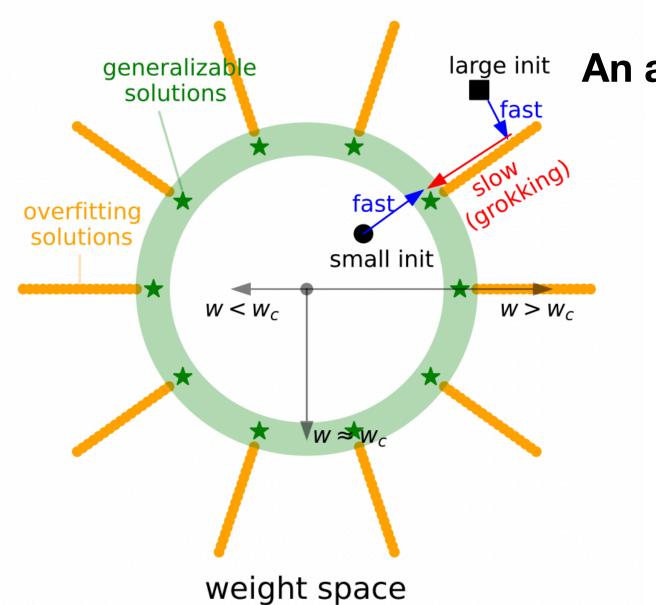




Phase diagrams of learning

Towards understanding grokking: An effective theory of representation learning

arXiv: 2205.10343 (NeurIPS 2022)



Microscopic

An adiabatic theory of learning dynamics

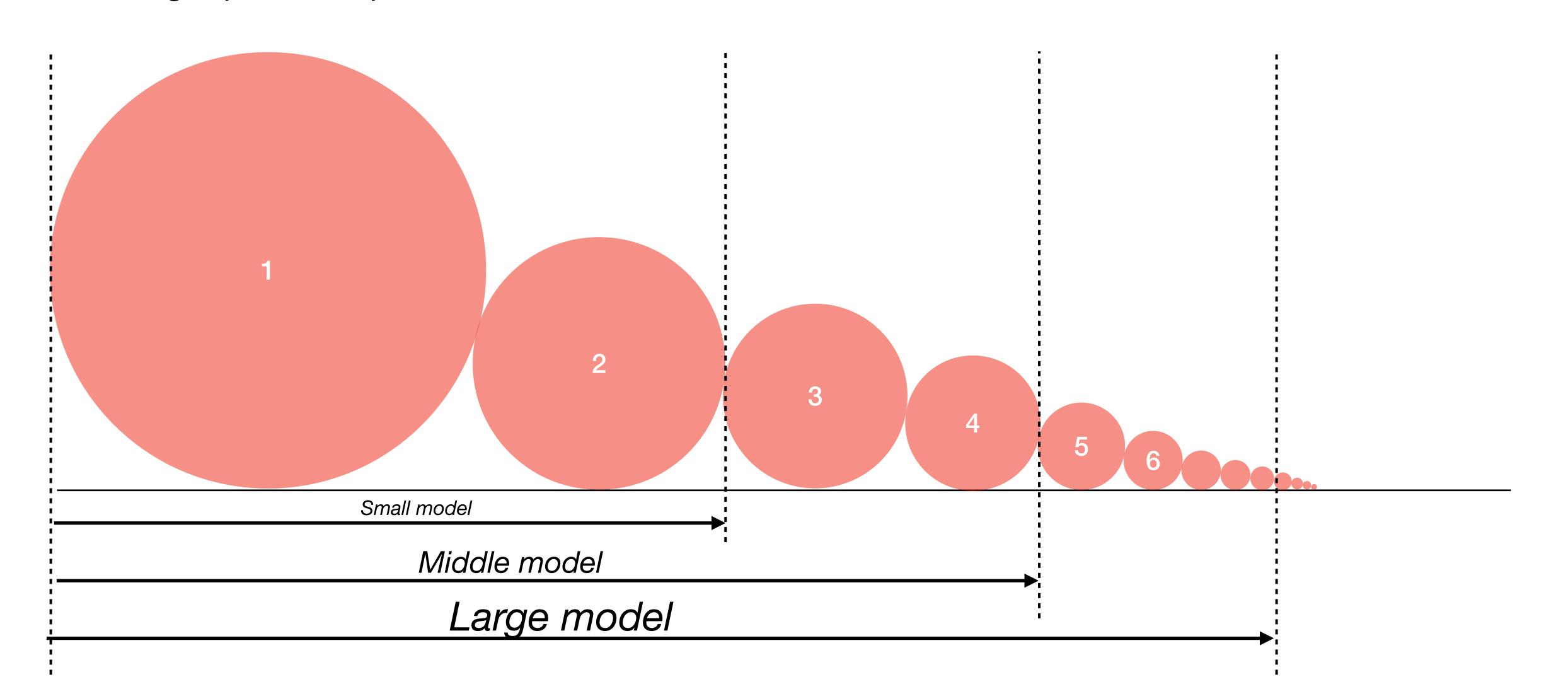
Omnigrok: Grokking Beyond Algorithmic data

arXiv: 2210.01117 (ICLR 2023)

Quantization of neural networks

Knowledge quanta sequence

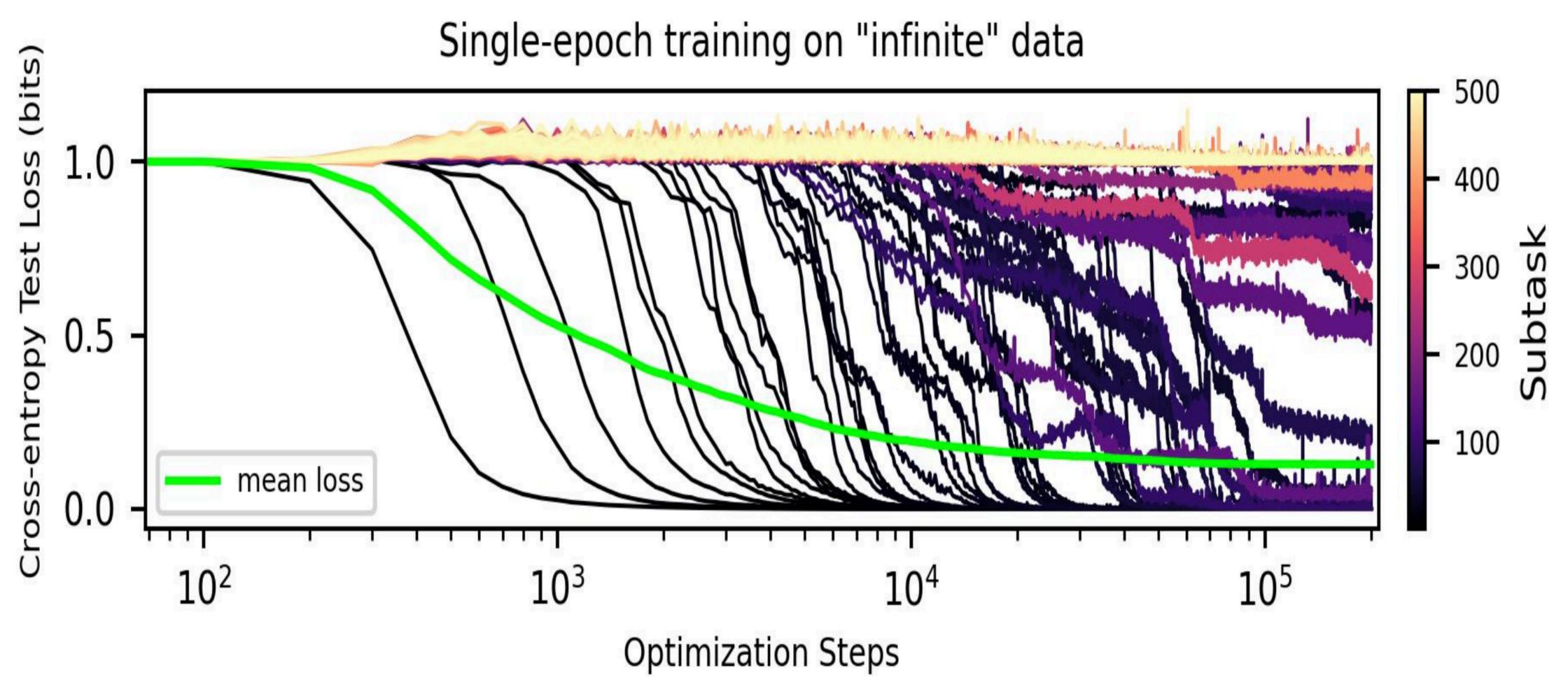
The quantisation model of neural scaling, arXiv: 2303.13506



Quantization of neural networks

A Quantization Model of Neural Scaling

arXiv: 2303.13506



Quantization of neural networks

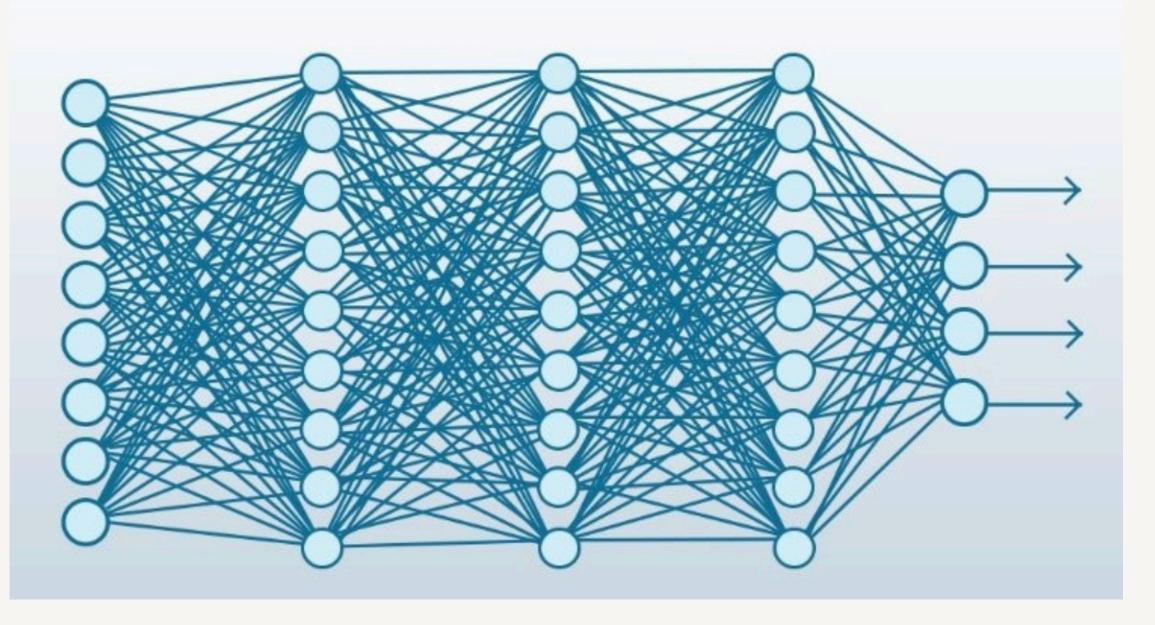
"Quanta" of LLM capabilities auto-discovered in natural text quantum for predicting newlines to maintain text width quantum for numerical sequence continuation (examples from cluster 50) (examples from cluster 100) ents his famous tonadas, a genre of the Venezuelan plains folk music. .C REGRESSION. THE GOALS OF THIS VIDEO ARE Track listing TO PERFORM QUADRATIC REGRESSION 01- Mi Querencia (Simón Díaz) ON THE TI84 GRAPHING CALCULATOR, DETERMINE HOW WELL THE 02- Tonada De Luna Llena (Simón Díaz) 03- Sabana (José Salazar/Simón Díaz) REGRESSION MODEL FITS THE DATA, 04- Caballo Viejo (Simón Díaz) AND THEN MAKE PREDICTIONS 05- Todo Este Campo Es Mío (Simón Díaz) USING THE REGRESSION EQUATION. IN STATISTICS, 06- La Pena Del Becerrero (Simón Díaz) REGRESSION ANALYSIS INCLUDES ANY TECHNIQUES USED FOR MODELING IN ...sis supplied.) Appealing from that order, the city asserts (1) plaintiffs have no standing or right to maintain the action; (2) that the ...ump is free software: you can redistribute it and/or modify proposed road was in an undedicated part of the park; (3) that the # it under the terms of the GNU General Public License as published by proposed road was an access road and not a through street or part of the # the Free Software Foundation, either version 3 of the License, or city's street system; (4 # (at your option) any later version. # creddump is distributed in the hope that it will be useful, \n Introduction_ 5. Chapter 1: What Is Trust? 6. Chapter 2: Trust Brings Rest Pursuant to 5TH CIR. R. 47.5, the court has determined 7. Chapter 3: Who Can I Trust? that this opinion should not be published and is not precedent 8. Chapter 4: The Folly of Self-Reliance except under the limited circumstances set forth in 5TH CIR.\n 9. Chapter 5: Trust God and Do Good (Part 1) 10. Chapter 6: Trust God and Do Good (Part 2) 11. Chapter 7: At All Times files (the 12. Chapter 8 // "Software"), to deal in the Software without restriction, including // without limitation the rights to use, copy, modify, merge, publish, .gn of noncavitated lesion seen only when the tooth is dried; 2 = // distribute, sublicense, and/or sell copies of the Software, and to visible noncavitated lesion seen when wet and dry; 3 = microcavitation in permit enamel; 4 = noncavitated lesion extending into dentine seen as an // persons to whom the Software is furnished to do so, subject to the \n undermining shadow; 5 = small cavitated lesion with visible dentine: less <!-than 50% of surface; 6 * Copyright (c) 2019, The Android Open Source Project .DynamicKey><Action>F1</Action><Label>F1</Label></DynamicKey> <DynamicKey><Action>F2</Action><Label>F2</Label></DynamicKey> * Licensed under the Apache License, Version 2.0 (the "License"); <DynamicKey><Action>F3</Action><Label>F3</Label></DynamicKey> <DynamicKey><Action>F4</Action><Label>F4</Label></DynamicKey> * you may not use this file except in compliance with the License.\n <DynamicKey><Action>F5 ..f maturity and an underdeveloped GetPrepareVoteMsg sense of responsibility, leading to recklessness, impul- $= 0 \times 07$ sivity, and heedless risk-taking.... Second, children PreparevotesMsg GetQCBlockListMsg are more vulnerable... to negative influences and QCBlockListMsg = 0x0a outside pressures, including from their family and GetLatestStatusMsq = 0x0bpeers; they have limited contro[1] over their own envi-\n LatestStatusMsg = 0x0cPrepareBlockHashMsg = 0x0dGetViewChangeMsg = 0x0e PingMsg $= 0 \times 0 f$

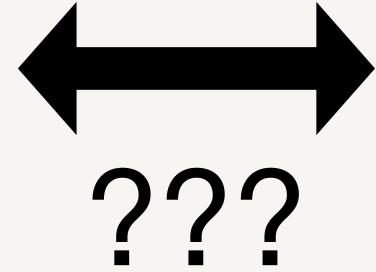
A Quantization Model of Neural Scaling

arXiv: 2303.13506

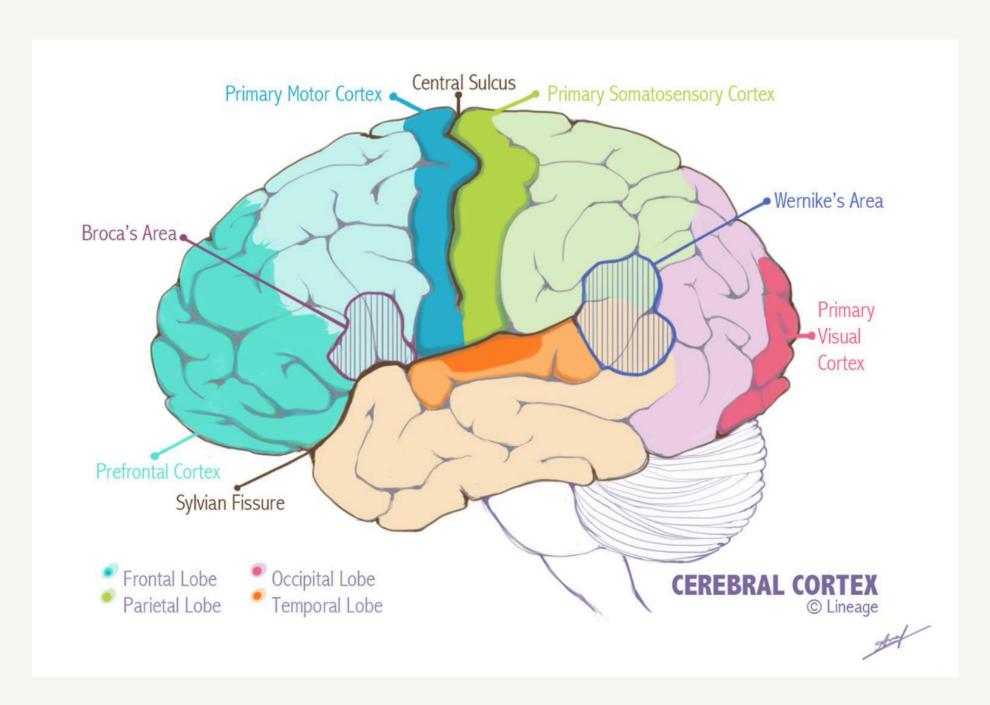
Neural networks vs brains

Neural networks





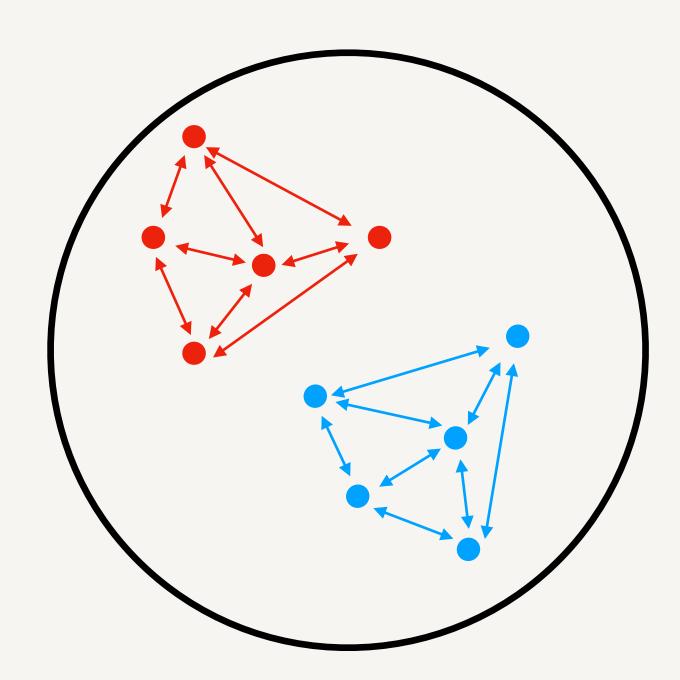
Brains



Modular brains have survival advantages, but modular NNs don't

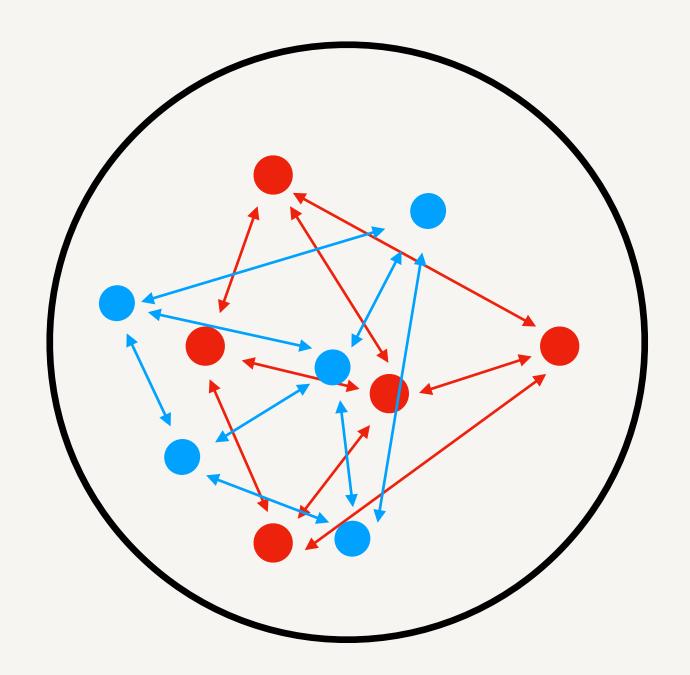
When humans deal with a specific task ...

Modular brains



Relevant neurons are local
Shorter neuron connections
React faster
More likely to survive

Non-Modular brains



Relevant neurons are non-local
Longer neuron connections
React slower
Less likely to survive

Q: Do modular neural networks have "survival advantages"?

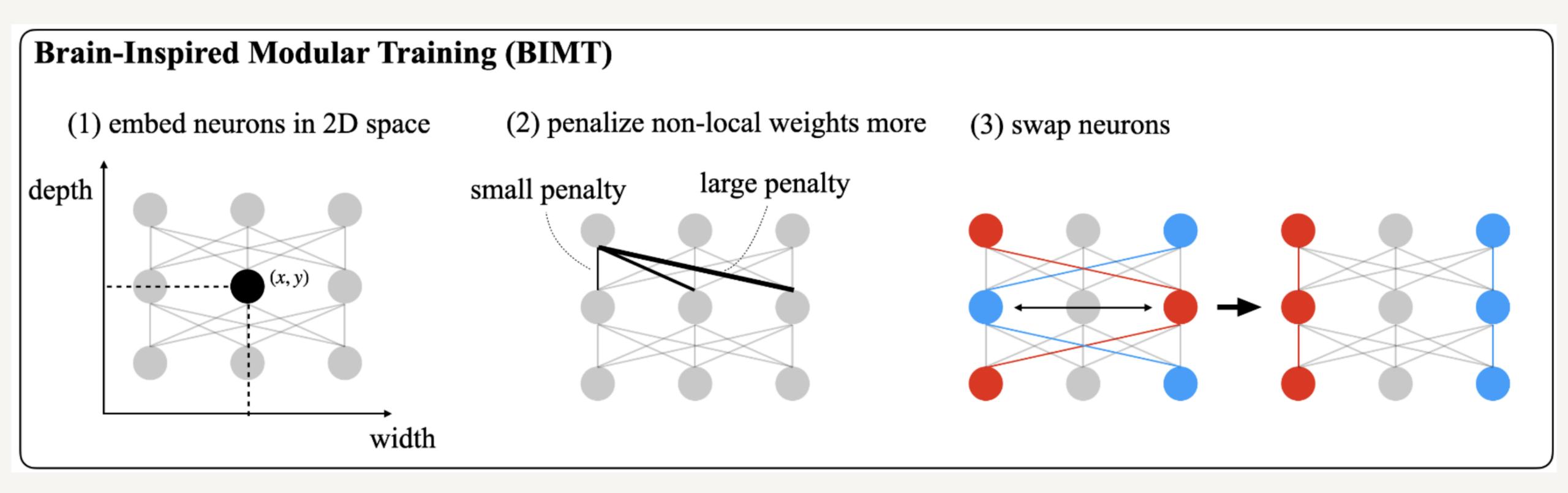
A: No! Because there is no (explicit) incentive for artificial neural networks to become modular if it only cares about prediction.

Q: What training techniques can induce modularity in otherwise non-modular networks?

A: Need to introduce "locality" and limit resources (hunger)!

Liu, Gan & Tegmark "Seeing is Believing: Brain-Inspired Modular Training for Mechanistic Interpretability"

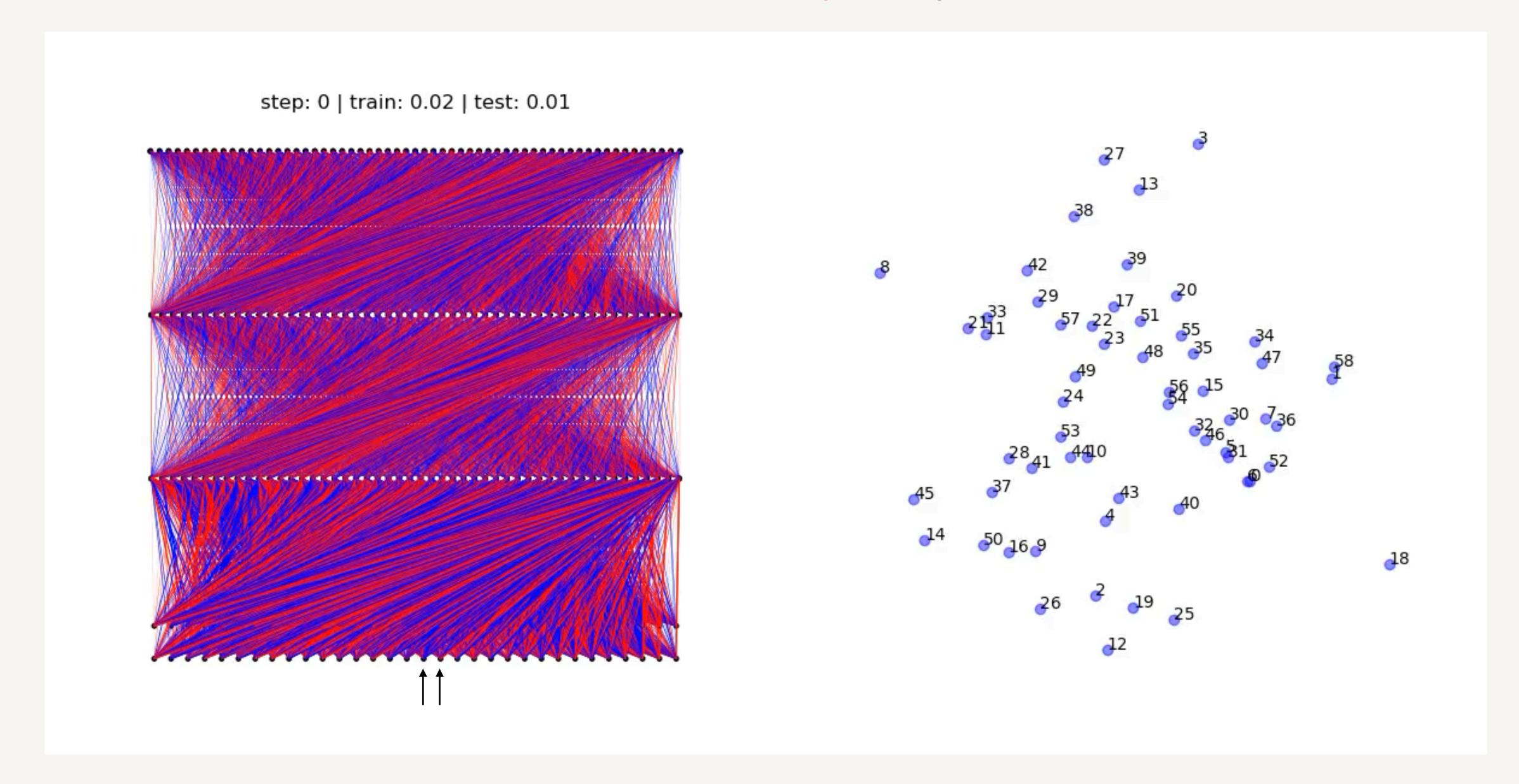
Brain-inspired modular training (BIMT)



Liu, Gan & Tegmark "Seeing is Believing: Brain-Inspired Modular Training for Mechanistic Interpretability" https://arxiv.org/abs/2305.08746

Modular addition

blue/red stands for positive/negative weights

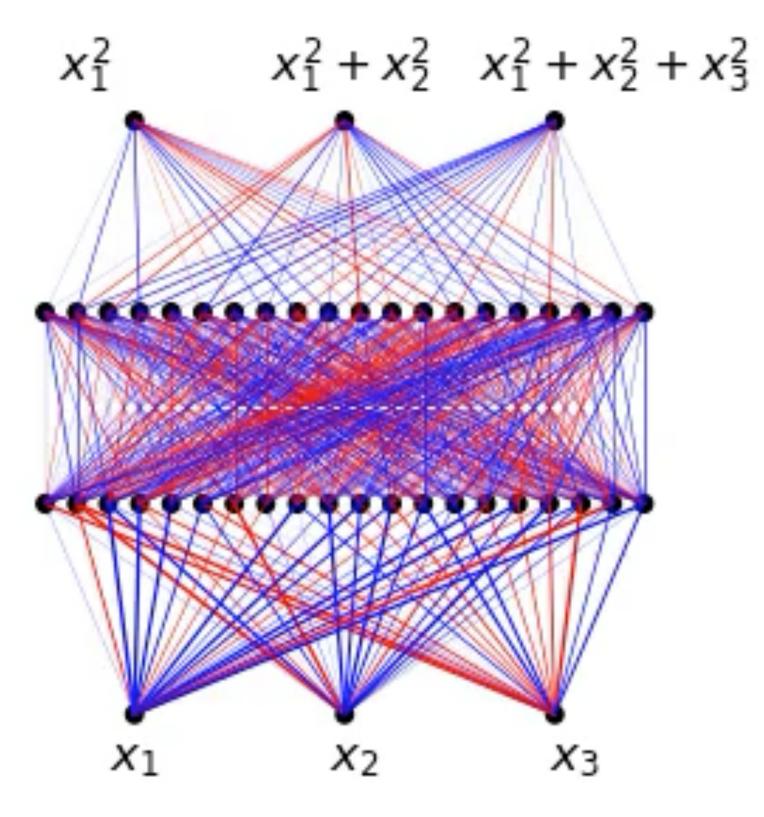


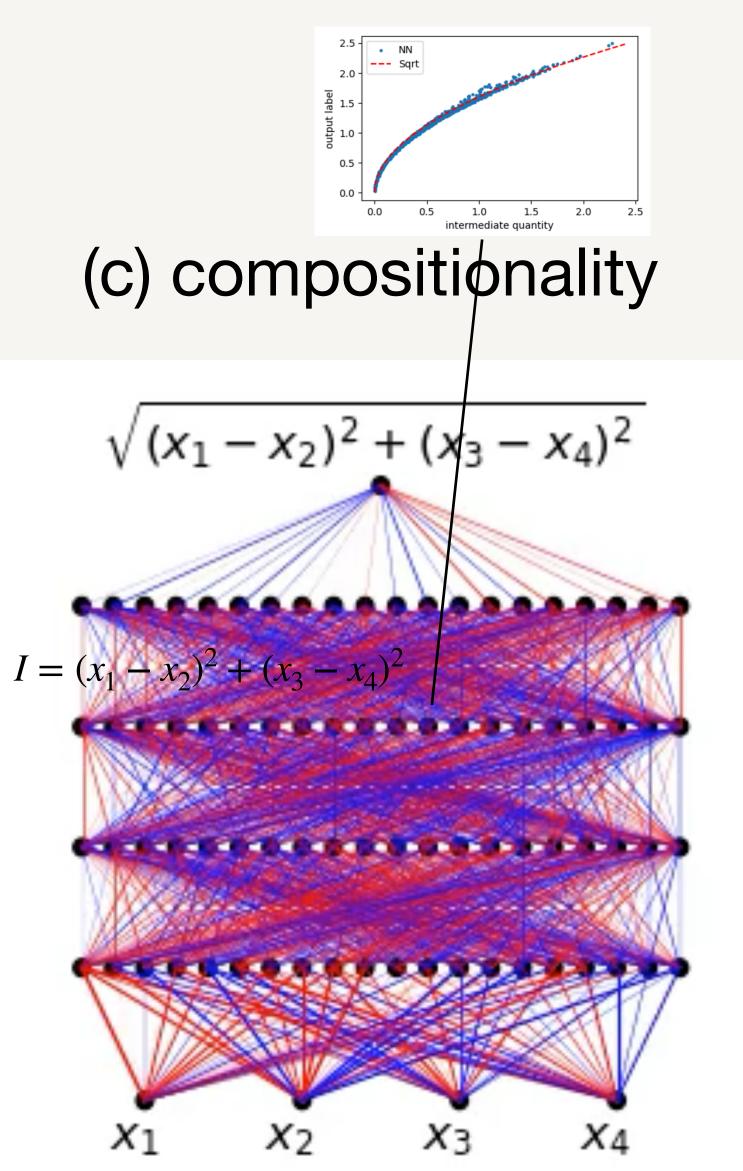
Symbolic formulas

(a) independence

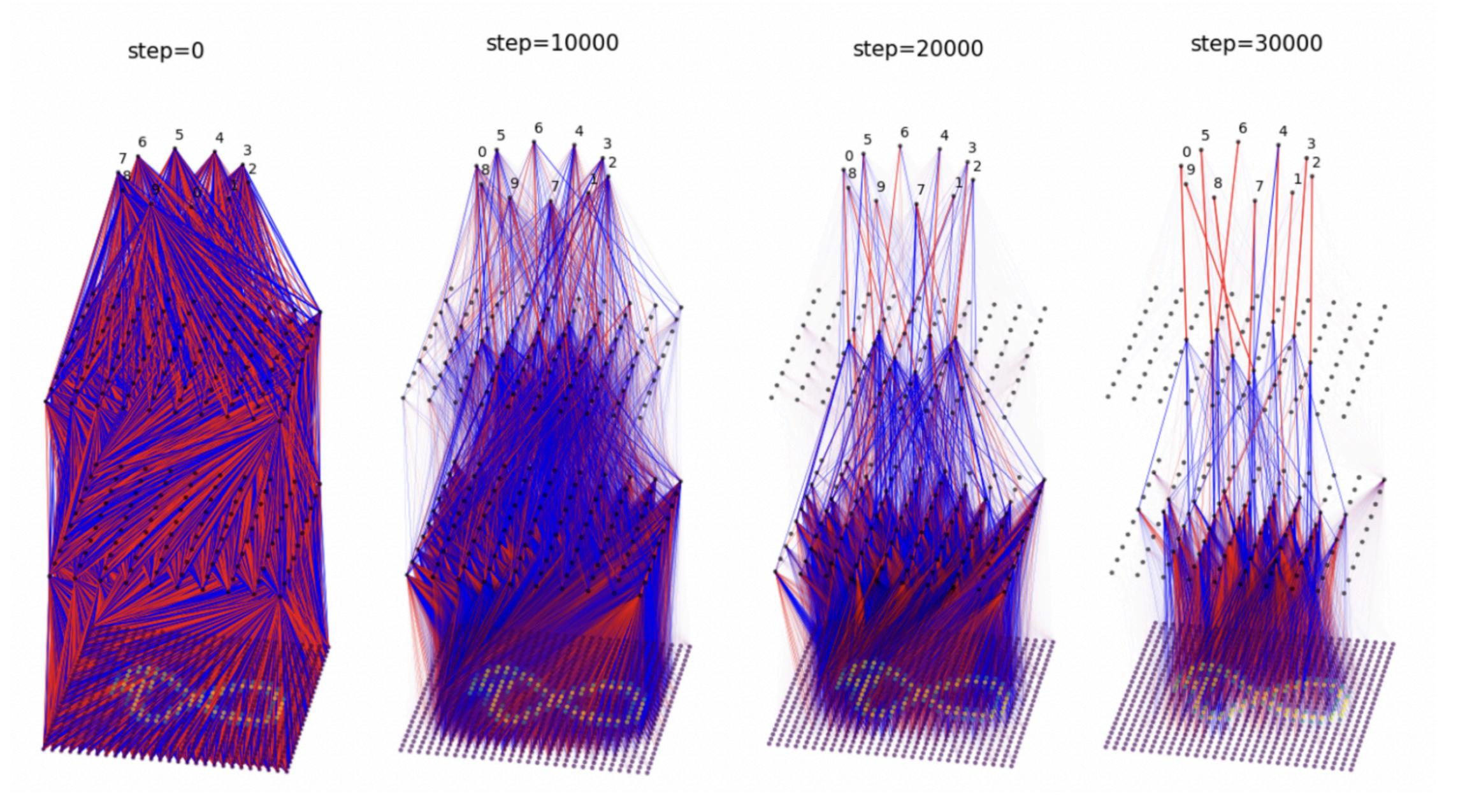
$$(x_1 + x_3)^3$$
 $x_2^2 + \sin(\pi x_4)$

(b) feature sharing





Locality/Modularity



Human scientists can survive in the time of Al

- The Survivors (幸存派) : admit AI has limitations, but reject AI. Humans can work in areas where AI has limitations. Do research areas that AI cannot solve.
- The Collaborators (合作派): admit AI has limitations, and accept AI. Only collaboration between AI and humans can lead to faster scientific development. Find research topics that neither AI nor human can solve.
- The Redemptionists (拯救派): admit AI has limitations, and improve AI. Use scientific tools to develop better AI.
- The Self-rescuers (自救派): concern about AI safety. Humans need to focus on AI safety so that we can better understand and finally control AI. Research on AI interpretability.
- The worshipers (崇拜派): Al is omnipotent, and embrace Al. Humans needn't and cannot understand Al. Just take advantage of Al power.
- The Adventists (降临派): Al is omnipotent, embrace Al and become Al. Align human values to Al, not the other way around. I don't know...

Note: Some of these beliefs are quite extreme. Most people lie on the continuous spectrum rather than extreme points.